

Lecture 3: Spectral Content

Zonghu Liao

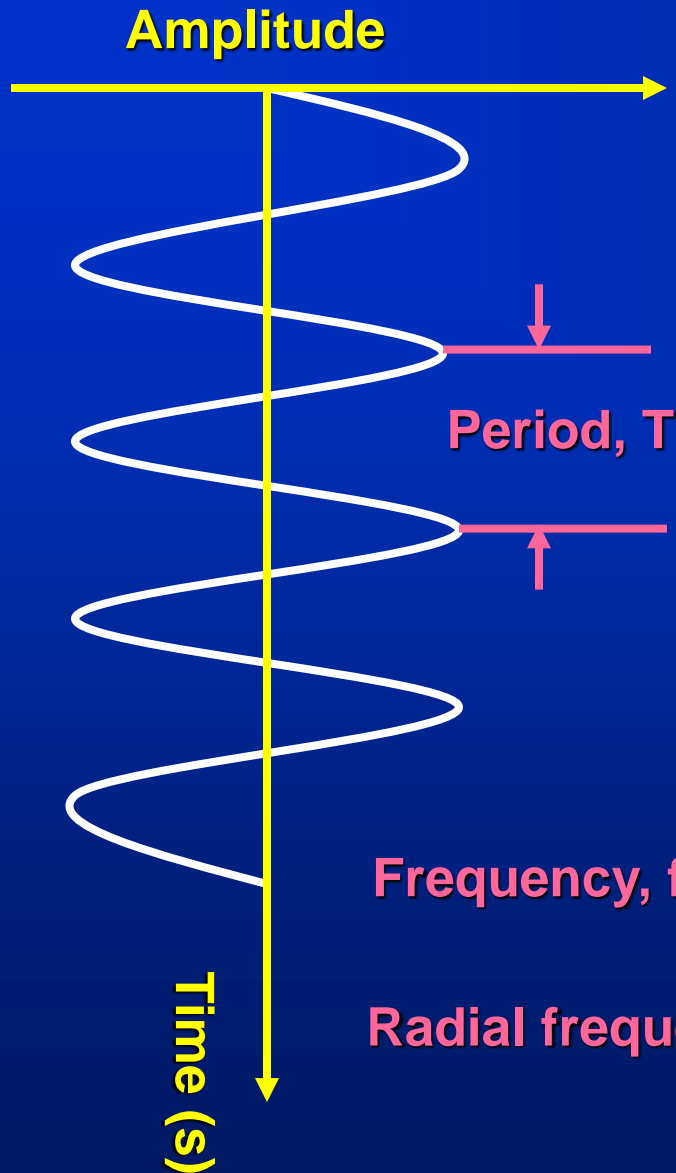
China University of Petroleum

Learner Objectives

After this section, you will be able to:

- **Visualize time- and space-variant signals in terms of their spectral components**
- **Be able to describe the impact of low-pass, high-pass, and band-pass filtering**
- **Evaluate strong, constructive interference from thin beds in terms of tuning thickness**

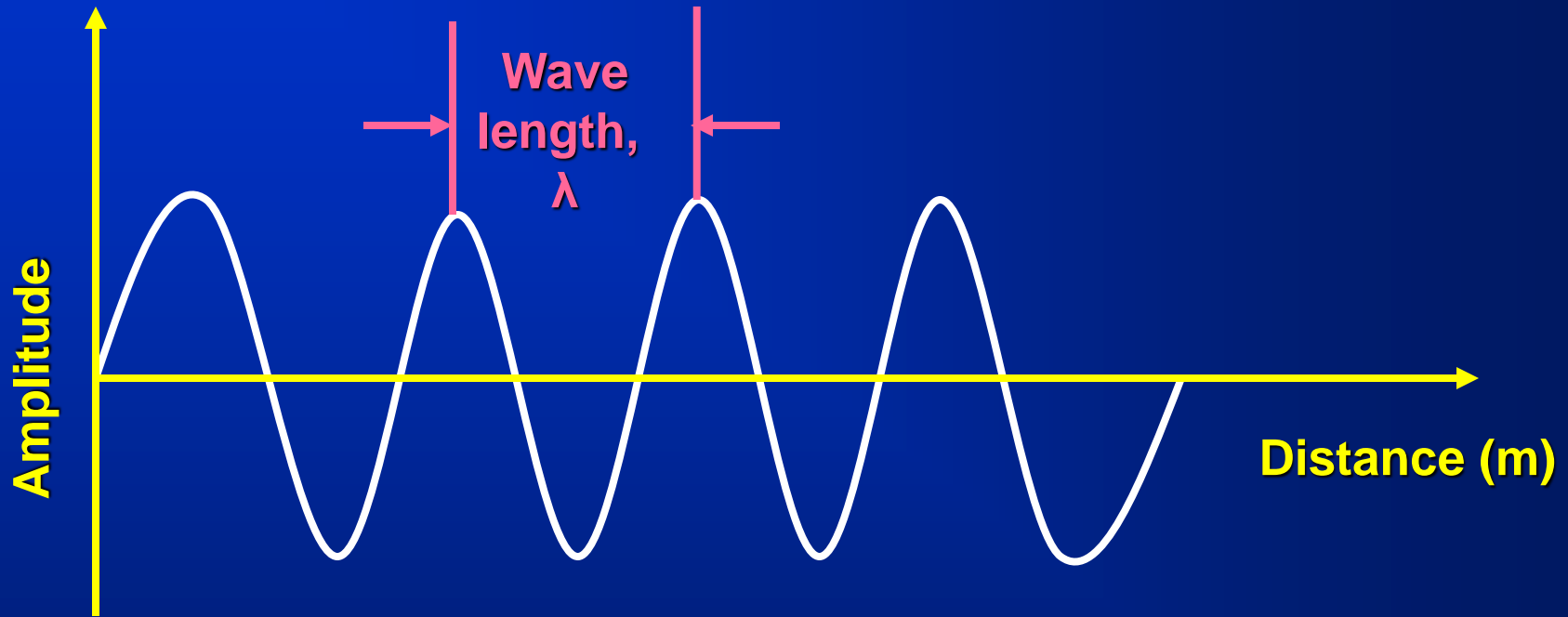
Periodic vibrations (in time)



Frequency, $f=1/T$ (measured in Hz)

Radial frequency, $\omega=2\pi f=2\pi/T$ (measured in radians/s)

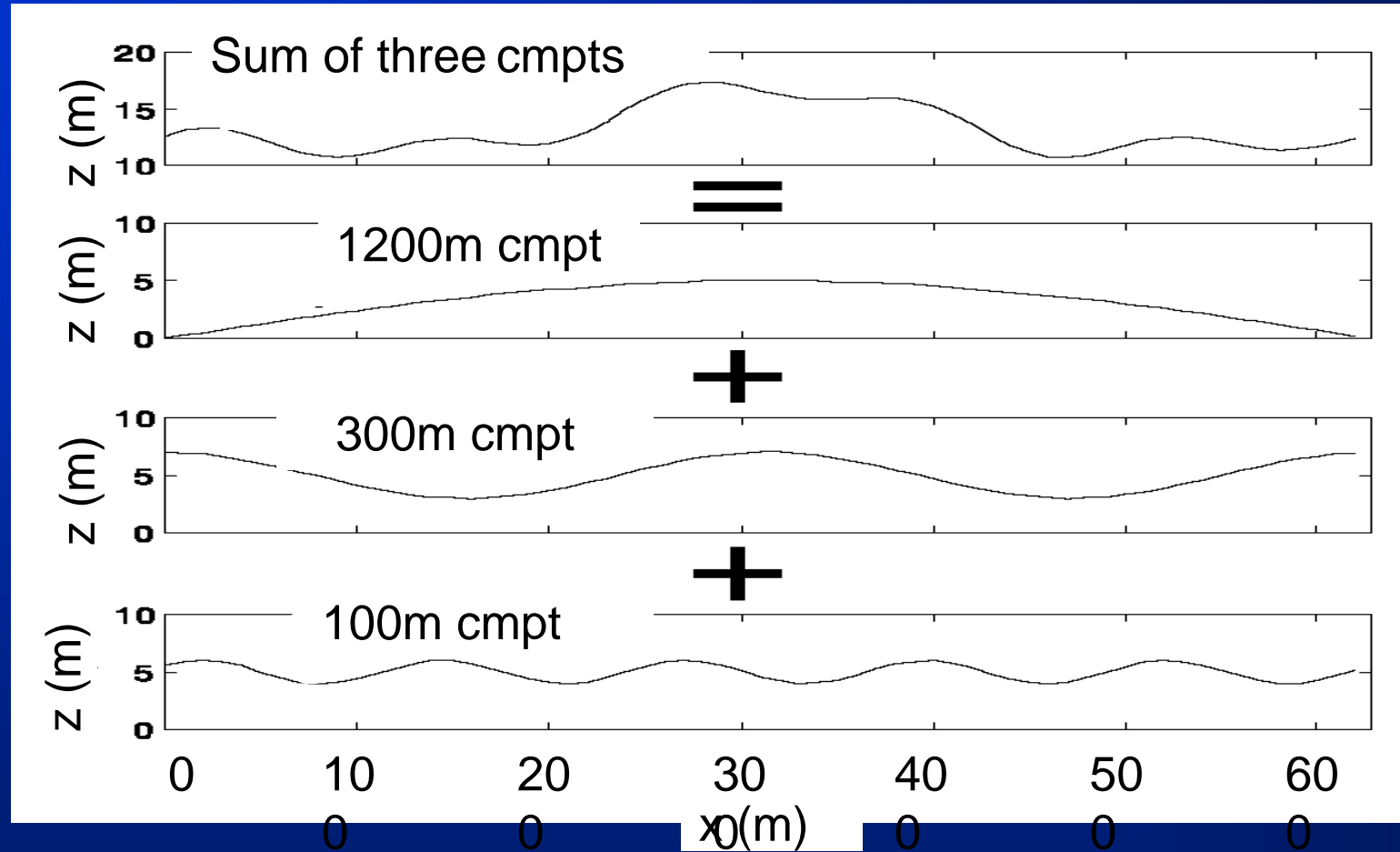
Periodic vibrations (in space)



Radial frequency, $\omega=2\pi /T$ (measured in Hz)

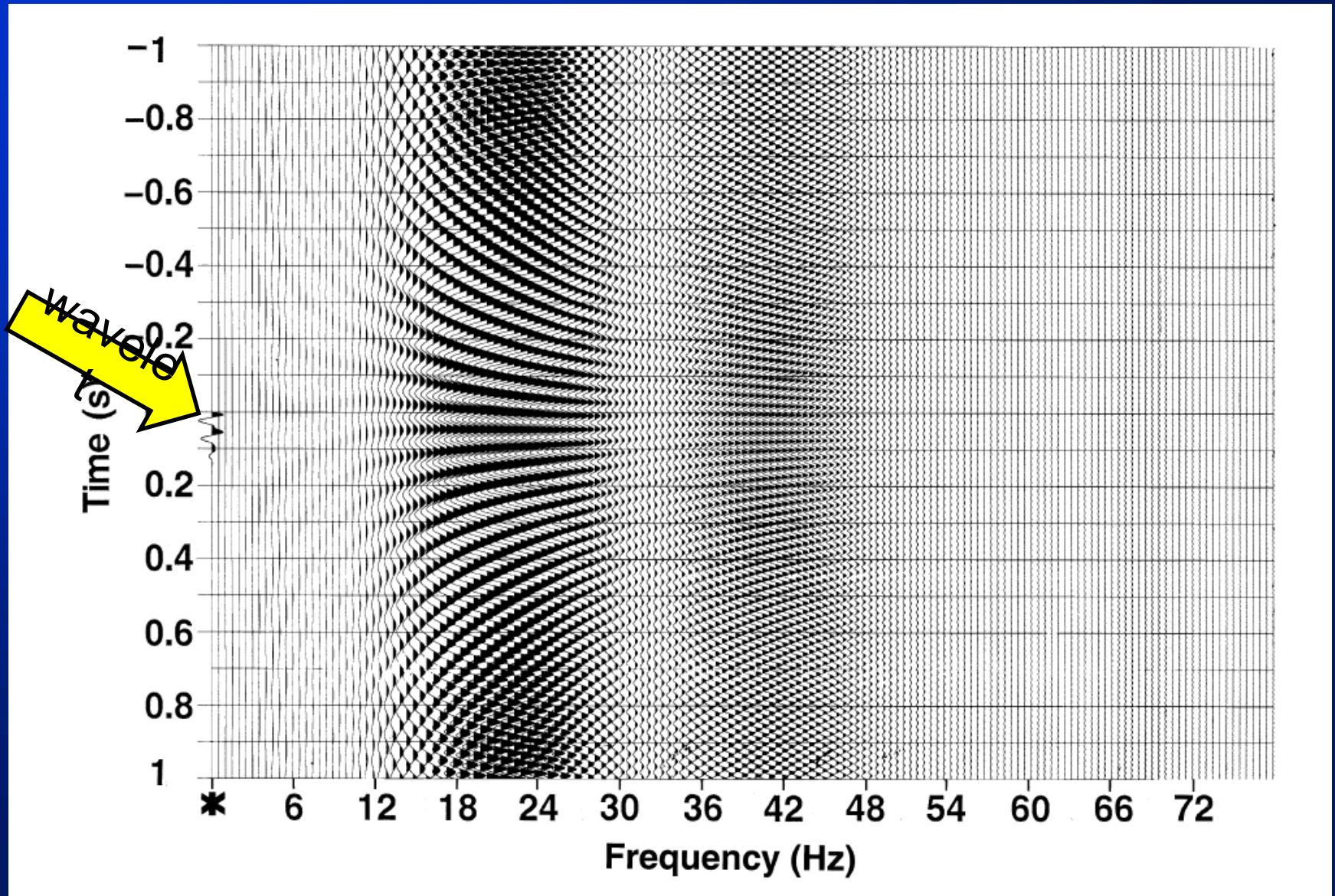
Wavenumber, $k=2\pi /\lambda$ (measured in radians/m)

Spectral analysis of topography



Any function can be decomposed into sinusoids of different amplitude, phase, and frequency.

Spectral analysis of a seismic wavelet



Forward Fourier Transforms

$$D_c(\omega) = \sum_{t=-T}^T d_{\text{even}}(t) \cos(\omega t) = \text{Fourier cosine transform}$$

$$D_s(\omega) = \sum_{t=0}^T d_{\text{odd}}(t) \sin(\omega t) \quad \text{Fourier sine transform}$$

$$D(\omega) = \sum_{t=0}^T d(t) \exp(+i\omega t) \quad \text{Complex Fourier transform}$$

$$D(\omega) = D_c(\omega) + iD_s(\omega)$$

Inverse Fourier Transforms

$$d_{\text{even}}(t) = \sum_{\omega=0}^{\omega_{\text{max}}} D_c(\omega) \cos(\omega t) \quad \text{Fourier cosine transform}$$

$$d_{\text{odd}}(t) = - \sum_{\omega=0}^{\omega_{\text{max}}} D_s(\omega) \sin(\omega t) \quad \text{Fourier sine transform}$$

$$d(t) = \sum_{\omega=0}^{\omega_{\text{max}}} D(\omega) \exp(-i\omega t) \quad \text{Complex Fourier transform}$$

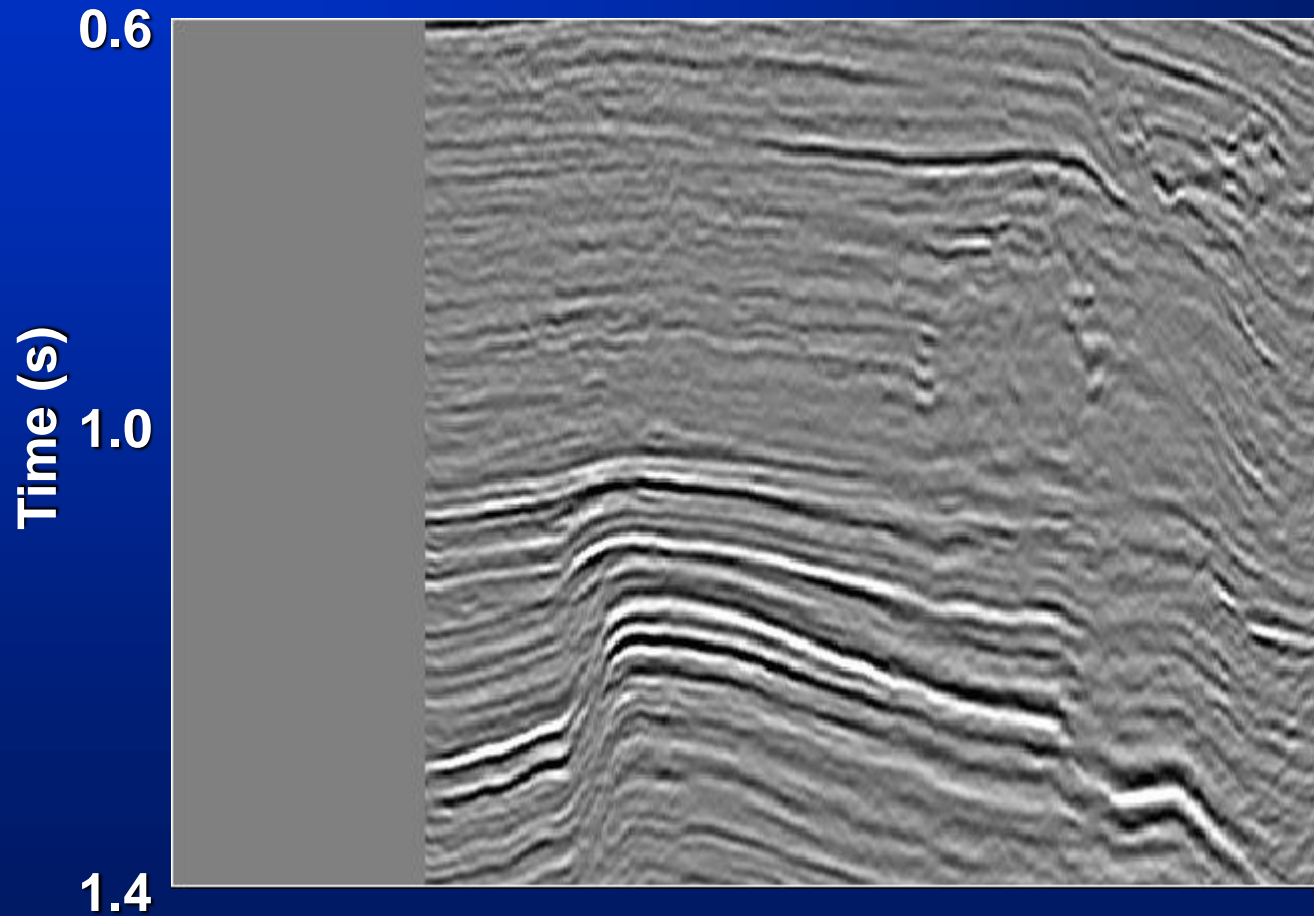
$$d(t) = d_{\text{even}}(t) + d_{\text{odd}}(t)$$

Wavelength



$$\lambda = \frac{v}{f} = \frac{10000\text{ft/s}}{50/\text{s}} = 200\text{ft}$$

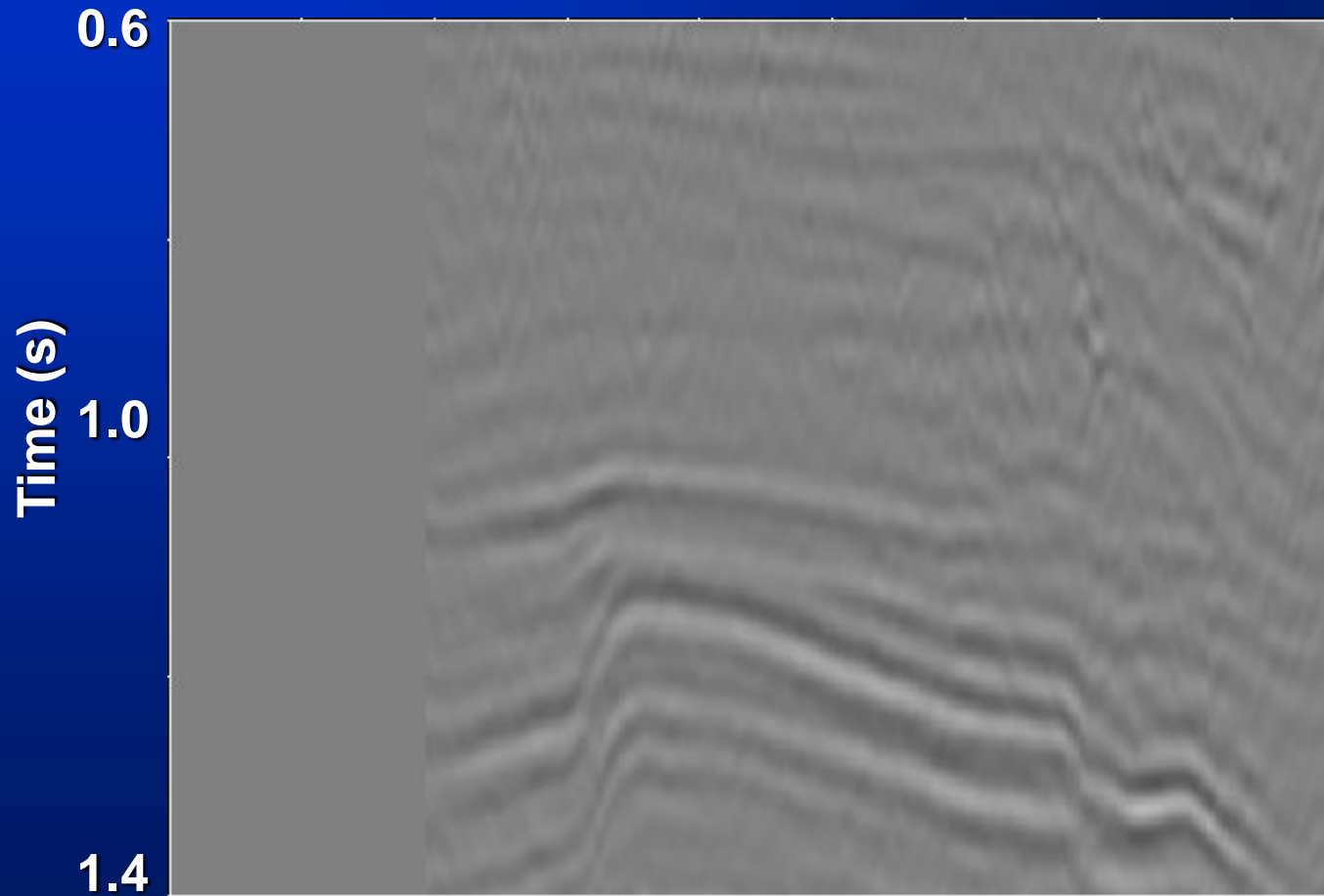
Original data (west Texas)



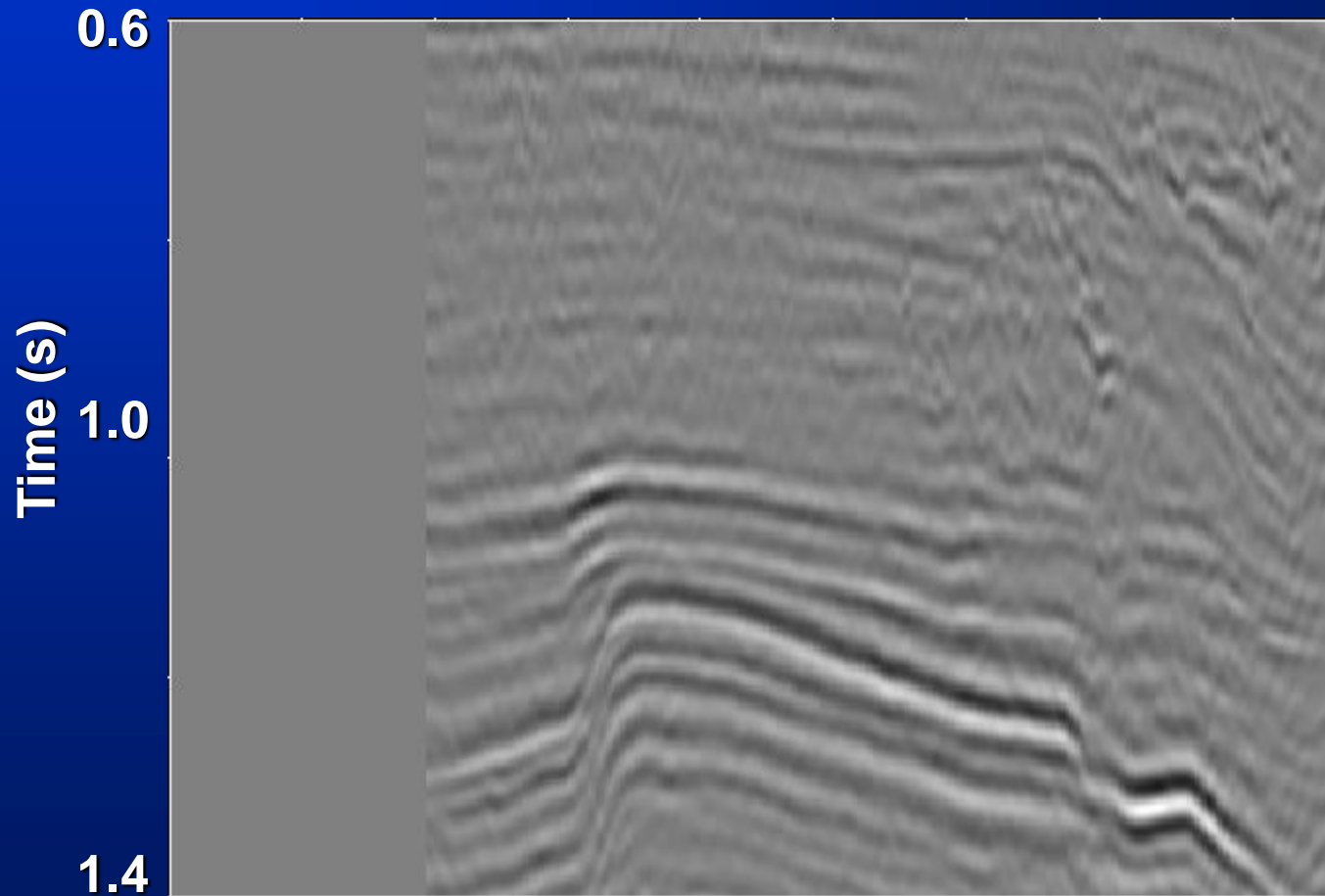
Low-pass filter ($f_{\text{high}}=10$ Hz)



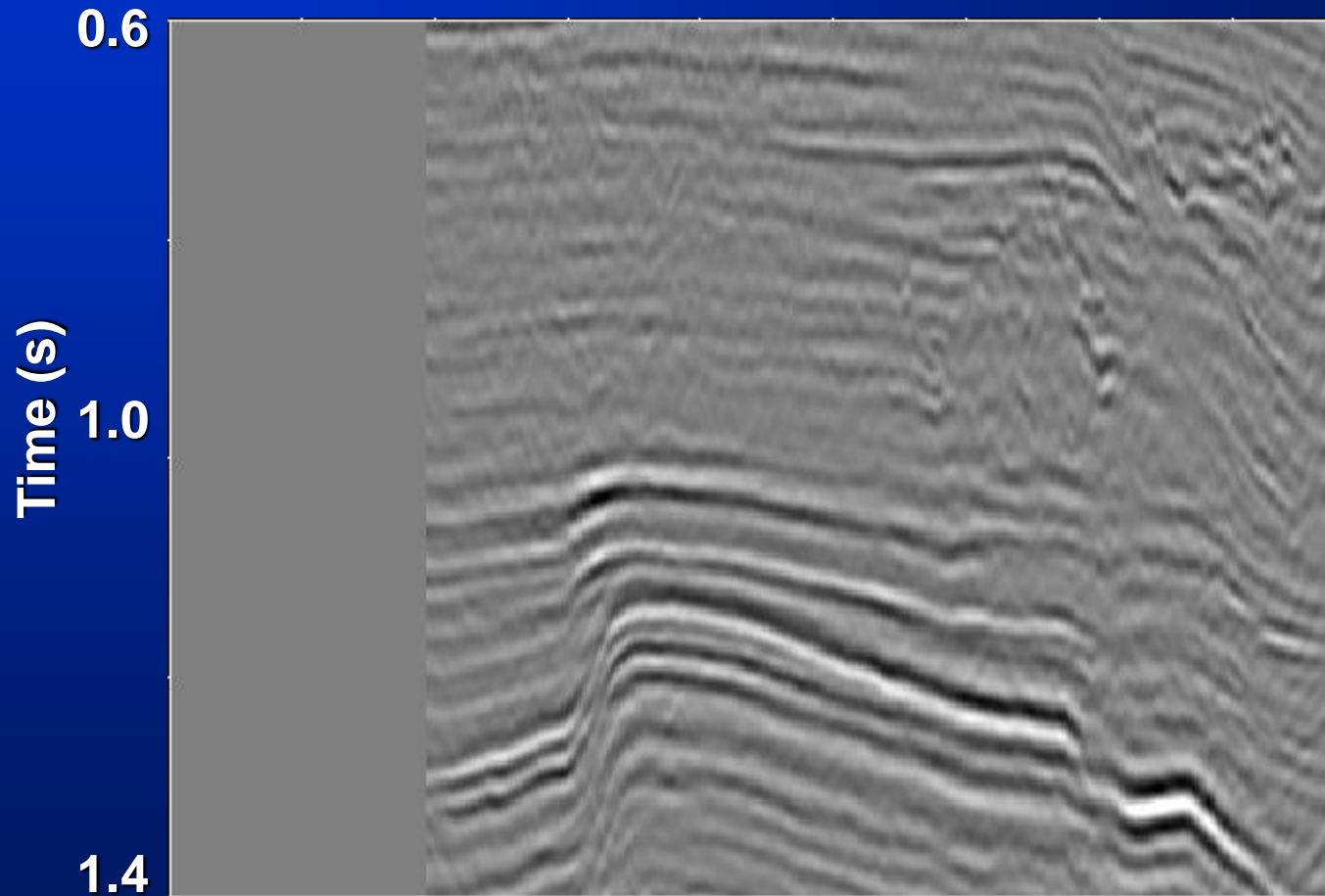
Low-pass filter ($f_{\text{high}}=20$ Hz)



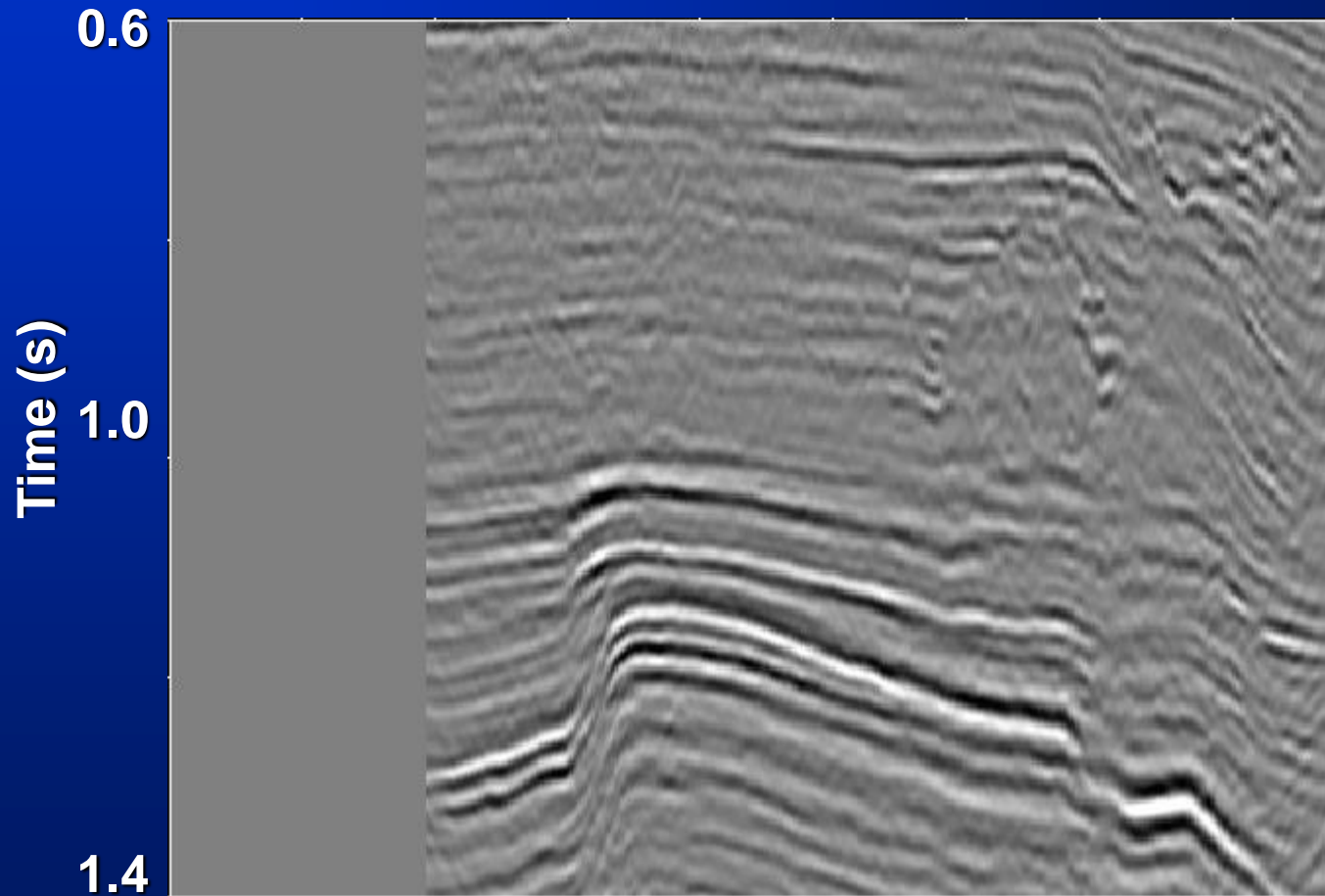
Low-pass filter ($f_{\text{high}}=30$ Hz)



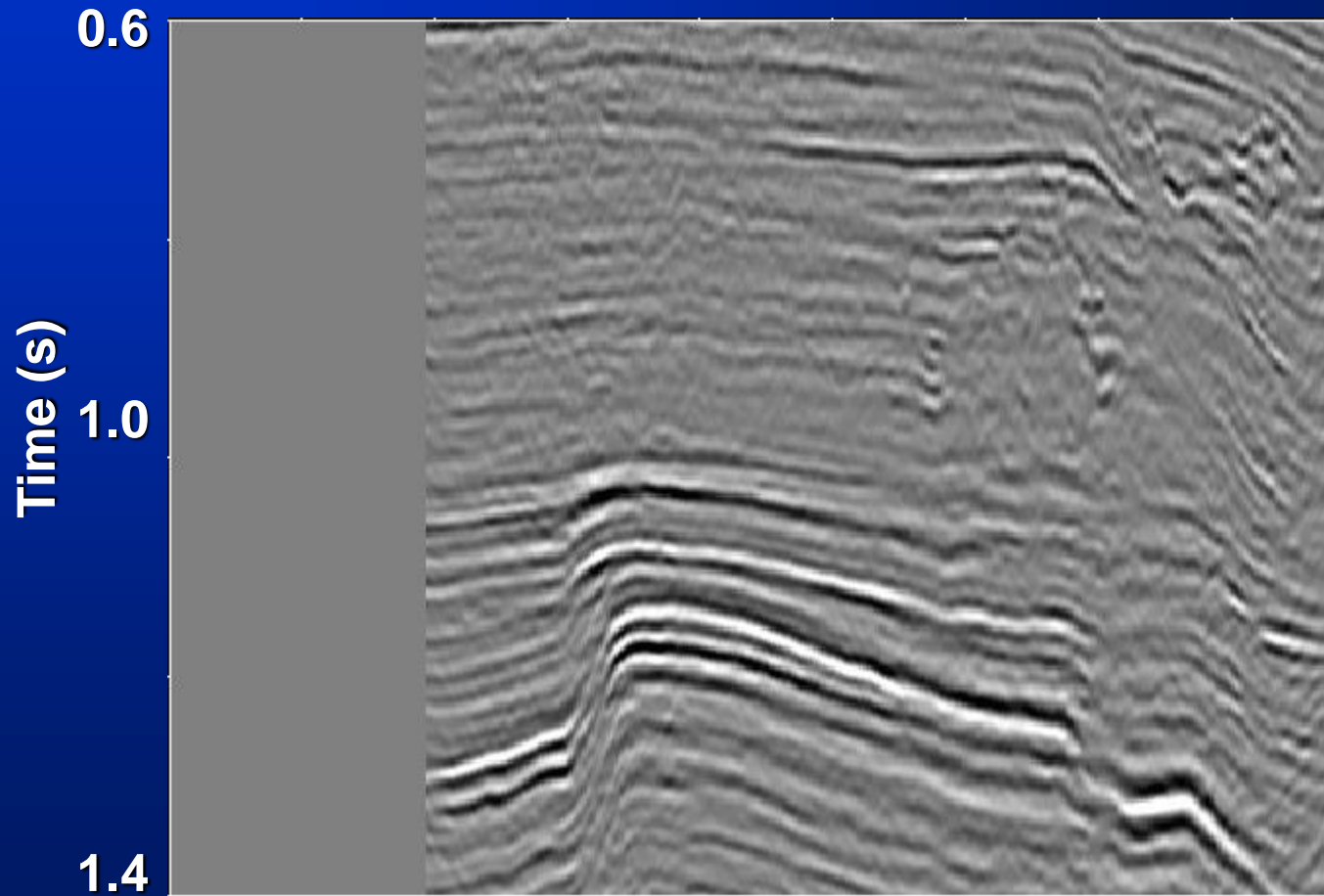
Low-pass filter ($f_{\text{high}}=40$ Hz)



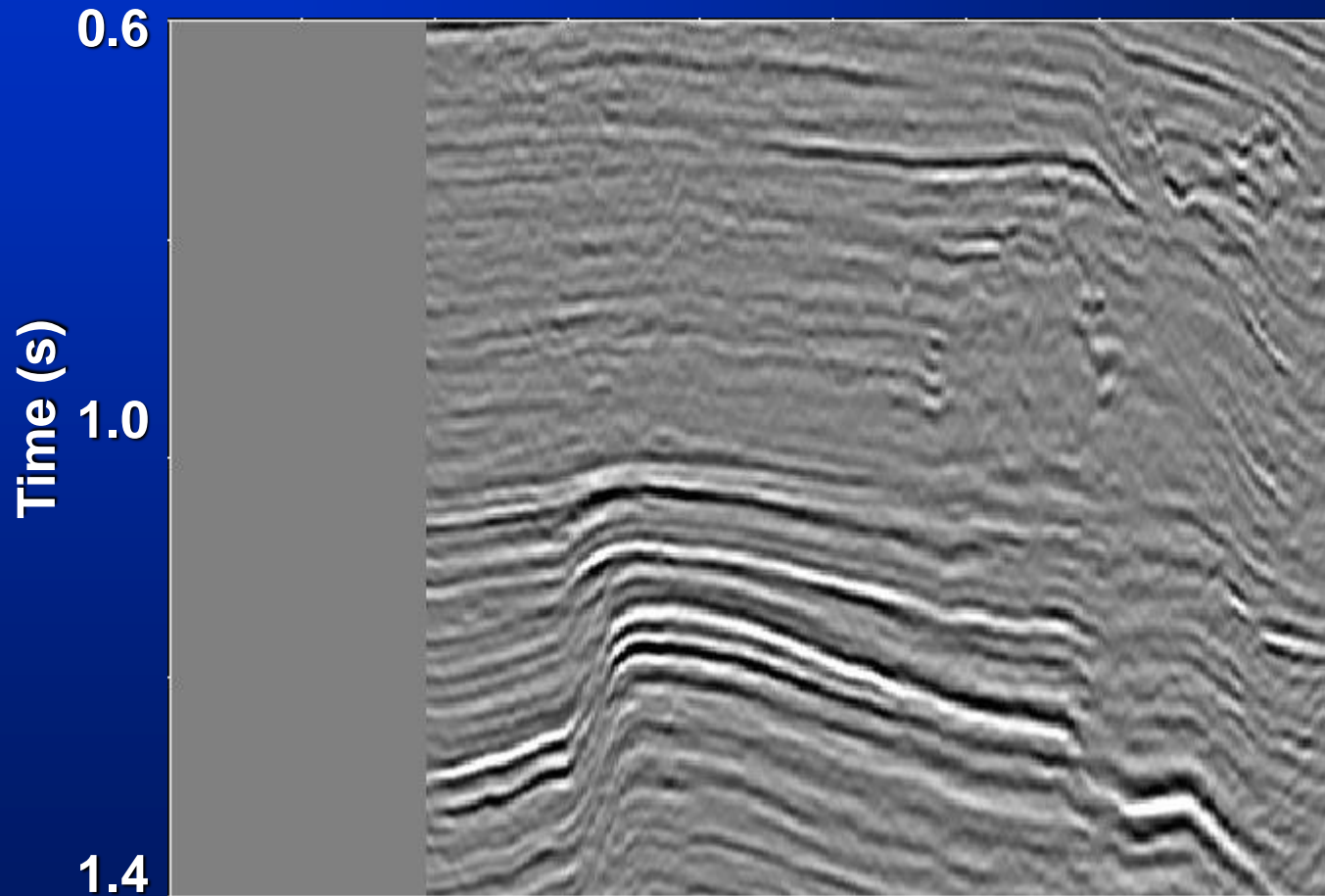
Low-pass filter ($f_{\text{high}}=50$ Hz)



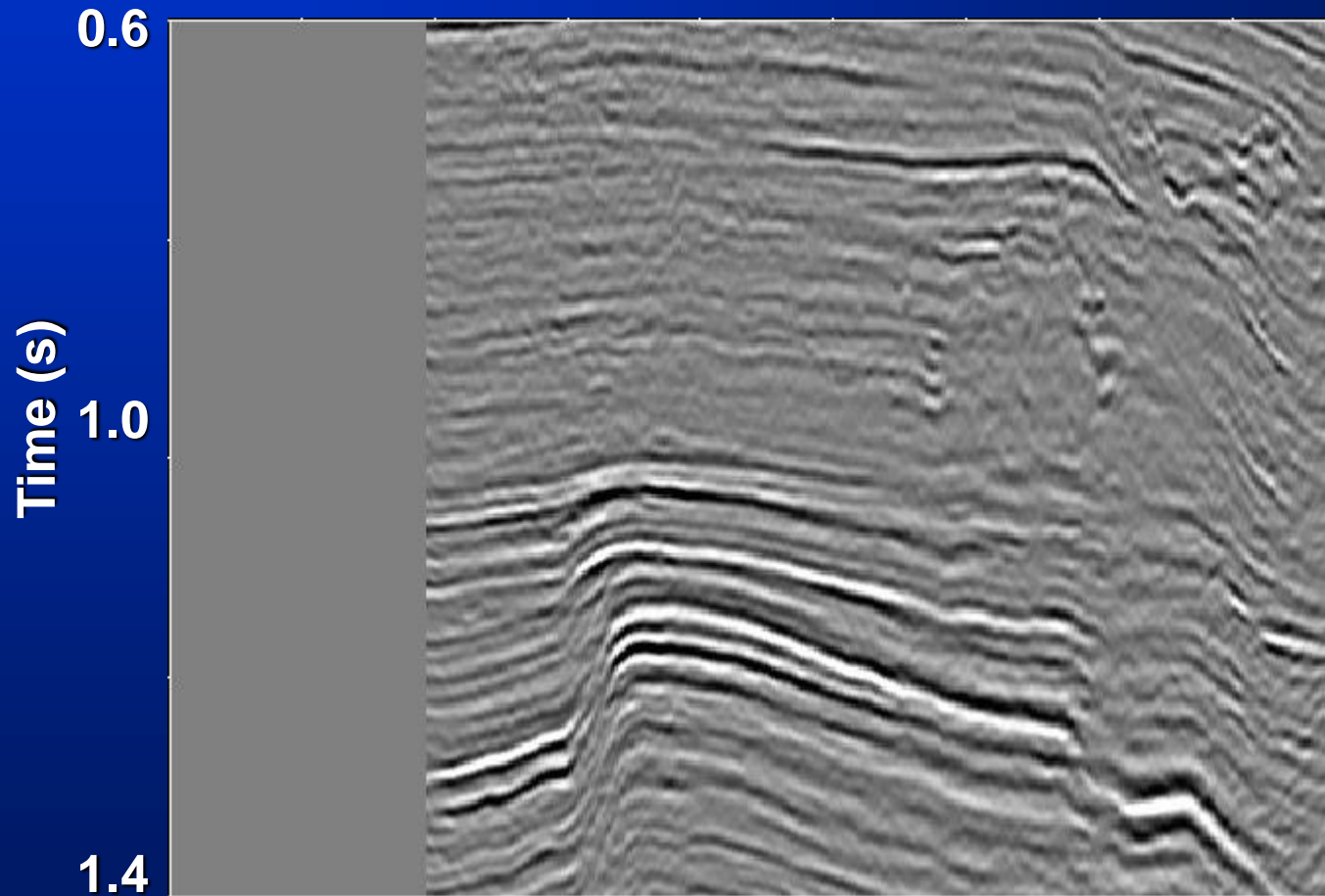
Low-pass filter ($f_{\text{high}}=60$ Hz)



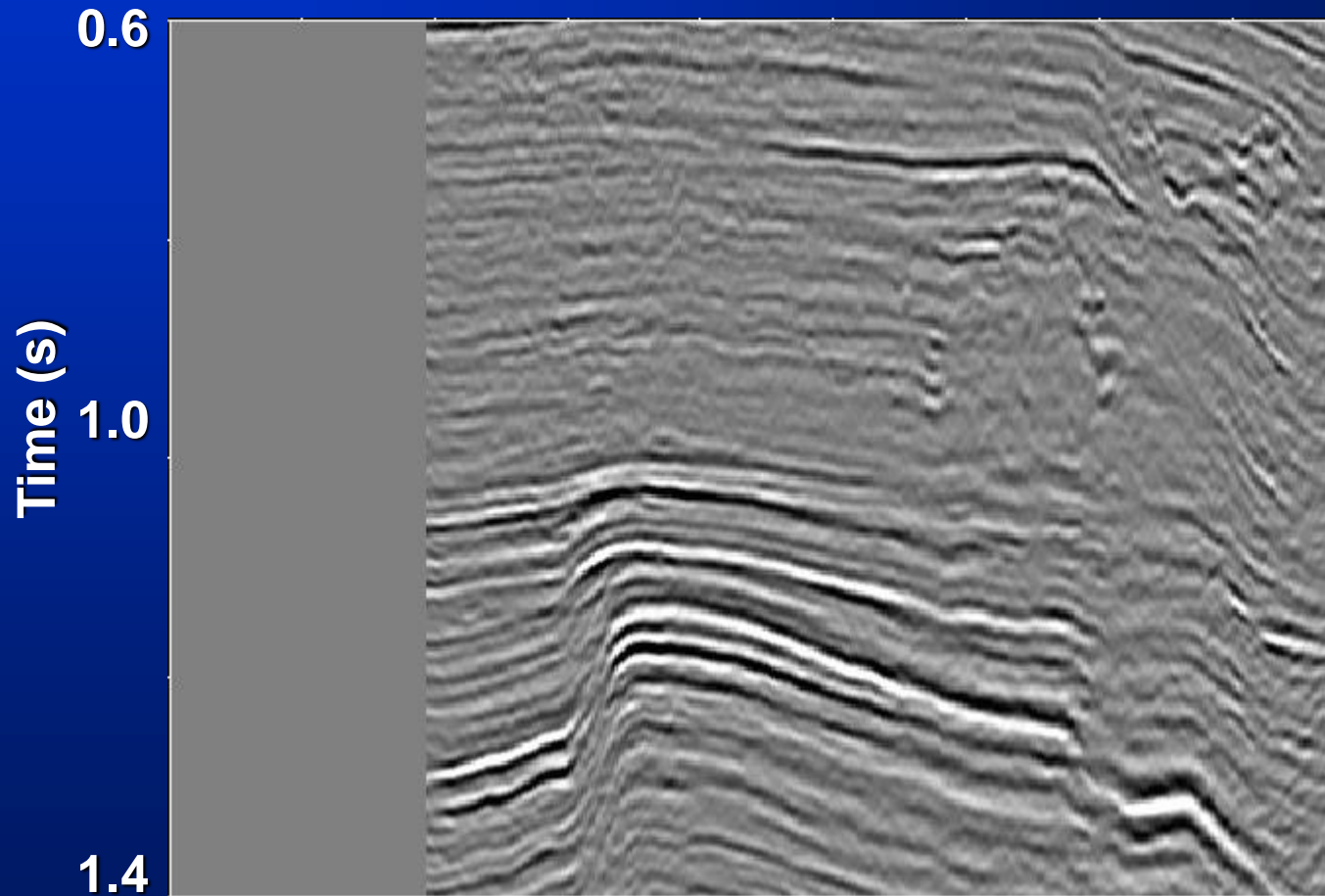
Low-pass filter ($f_{\text{high}}=70$ Hz)



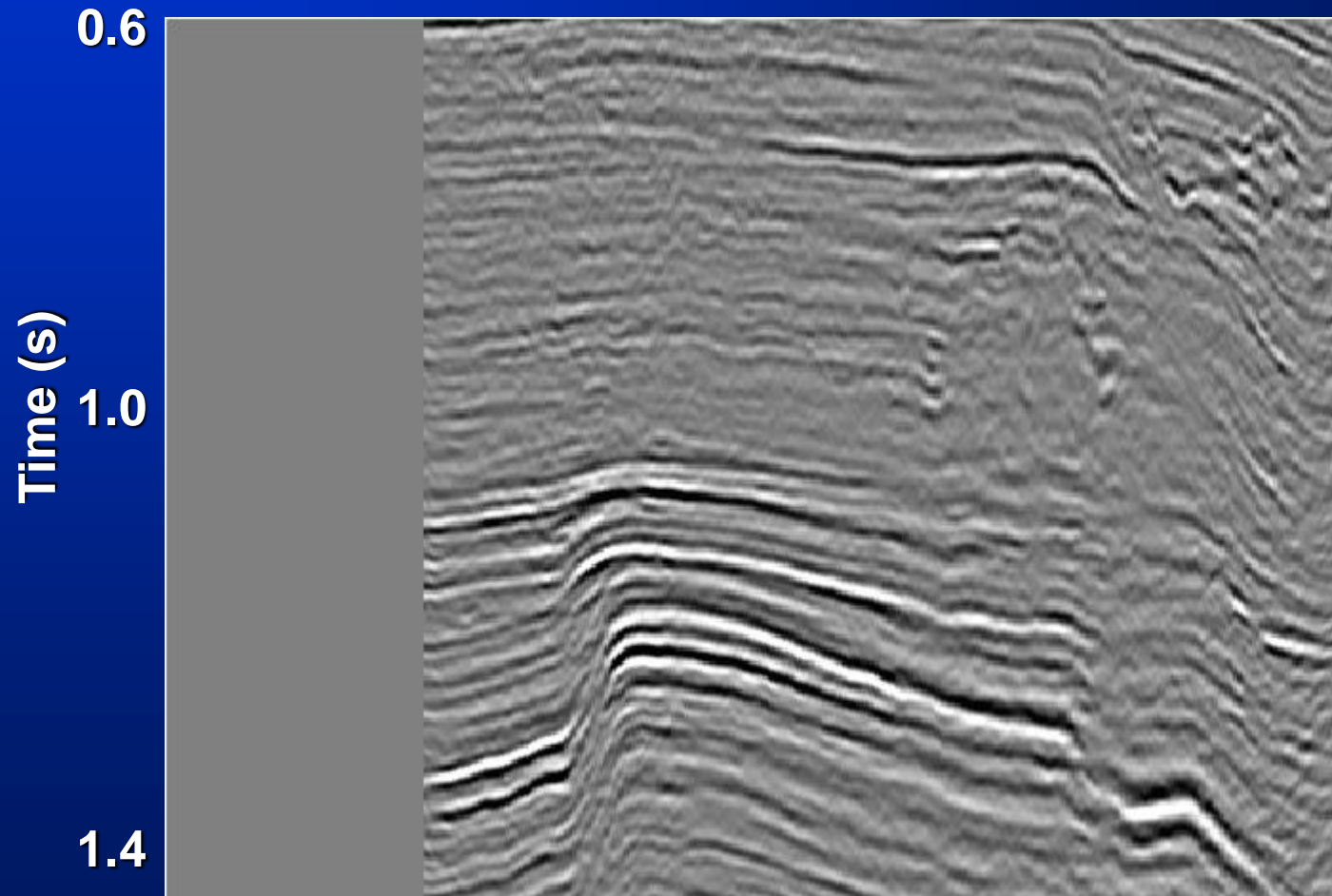
Low-pass filter ($f_{\text{high}}=80$ Hz)



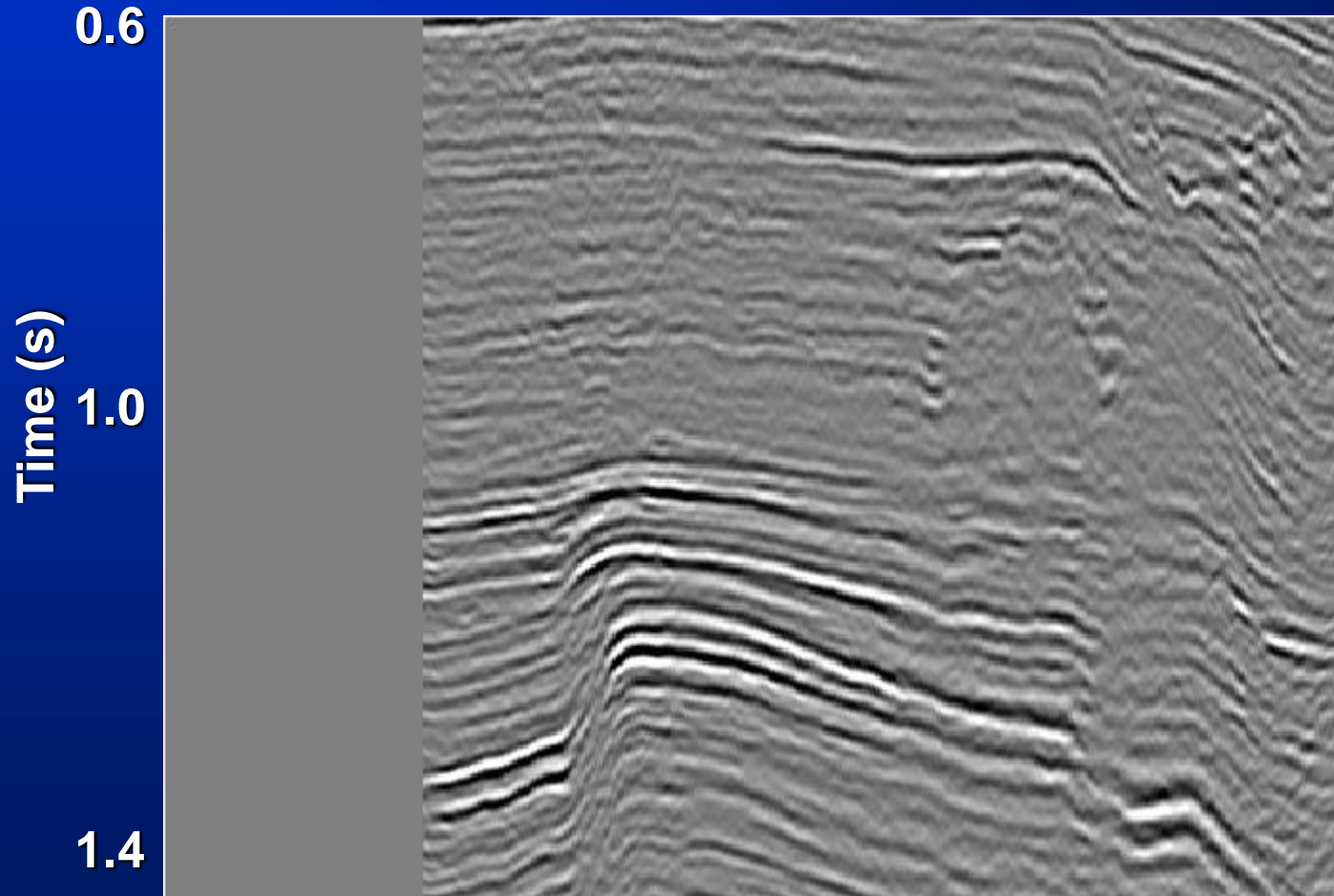
Low-pass filter ($f_{\text{high}}=90$ Hz)



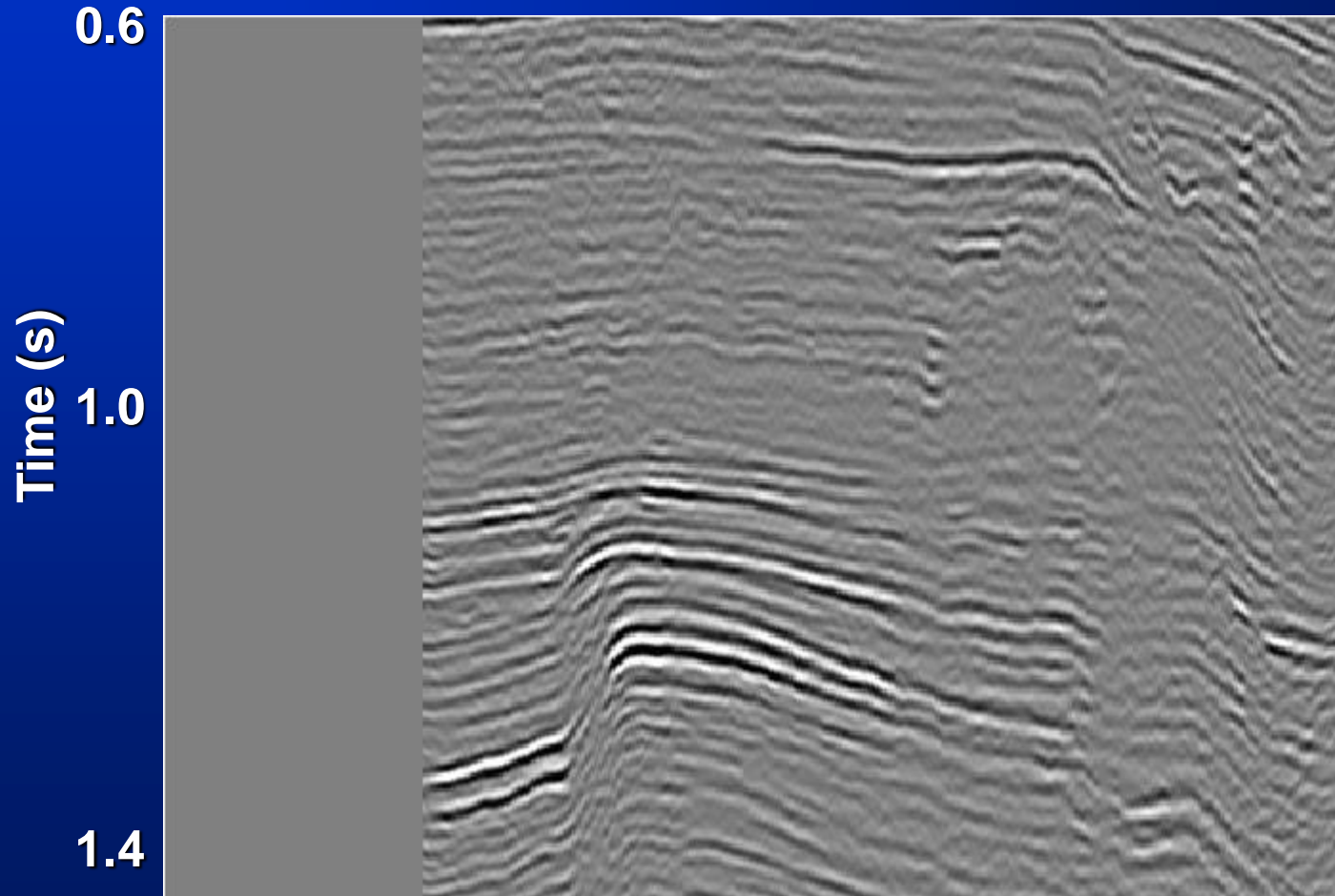
High-pass filter ($f_{low}=10$ Hz)



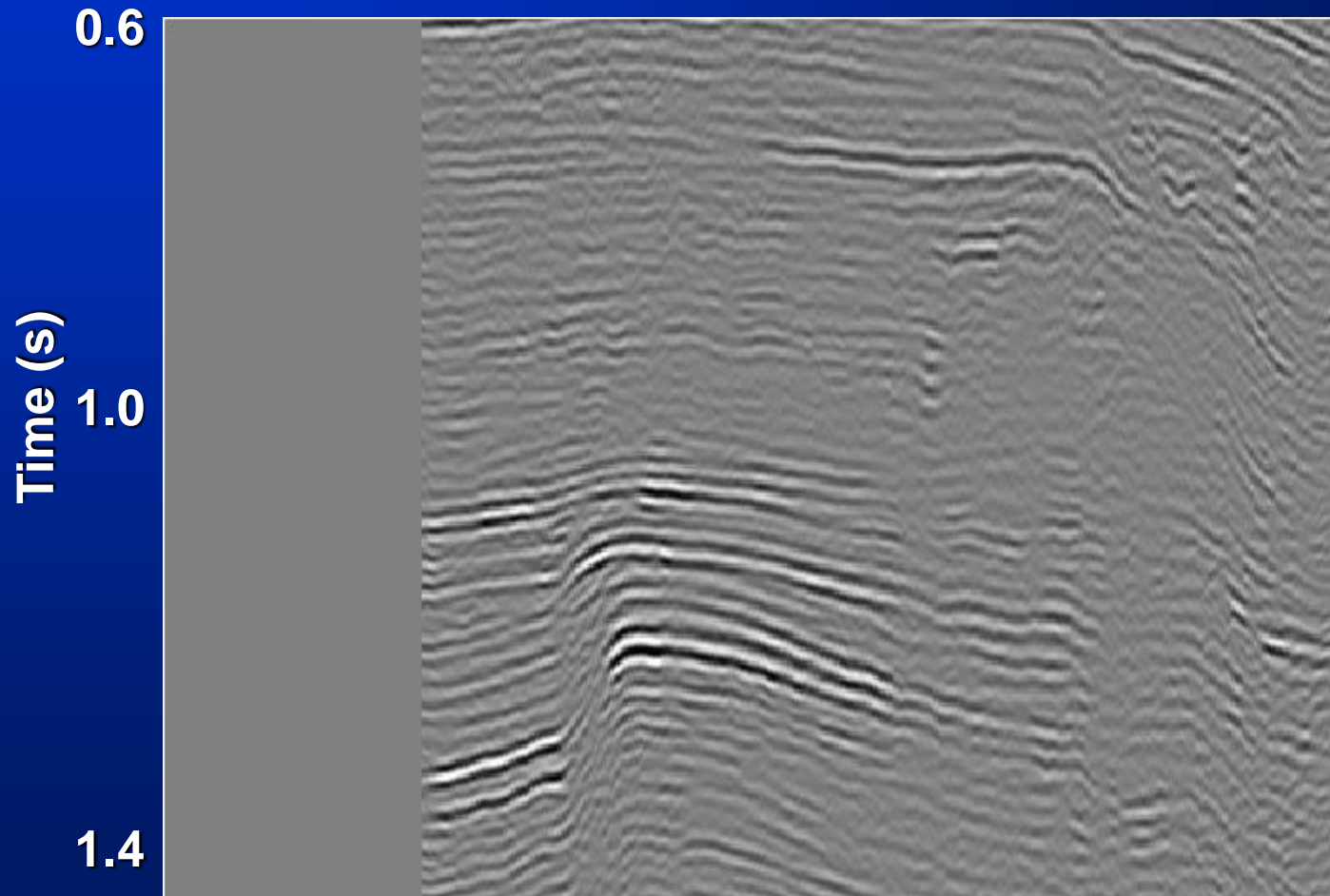
High-pass filter ($f_{low}=20$ Hz)



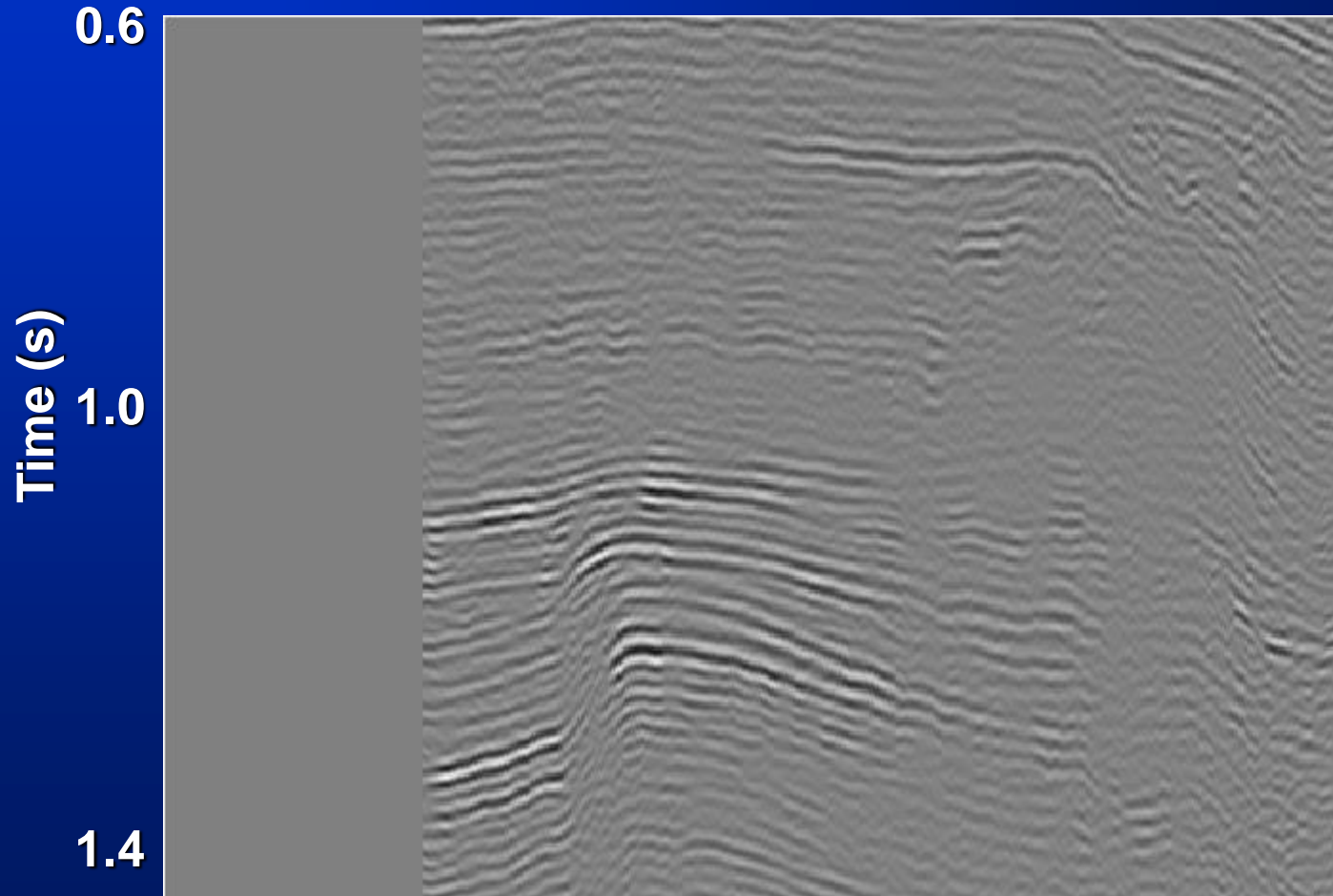
High-pass filter ($f_{low}=30$ Hz)



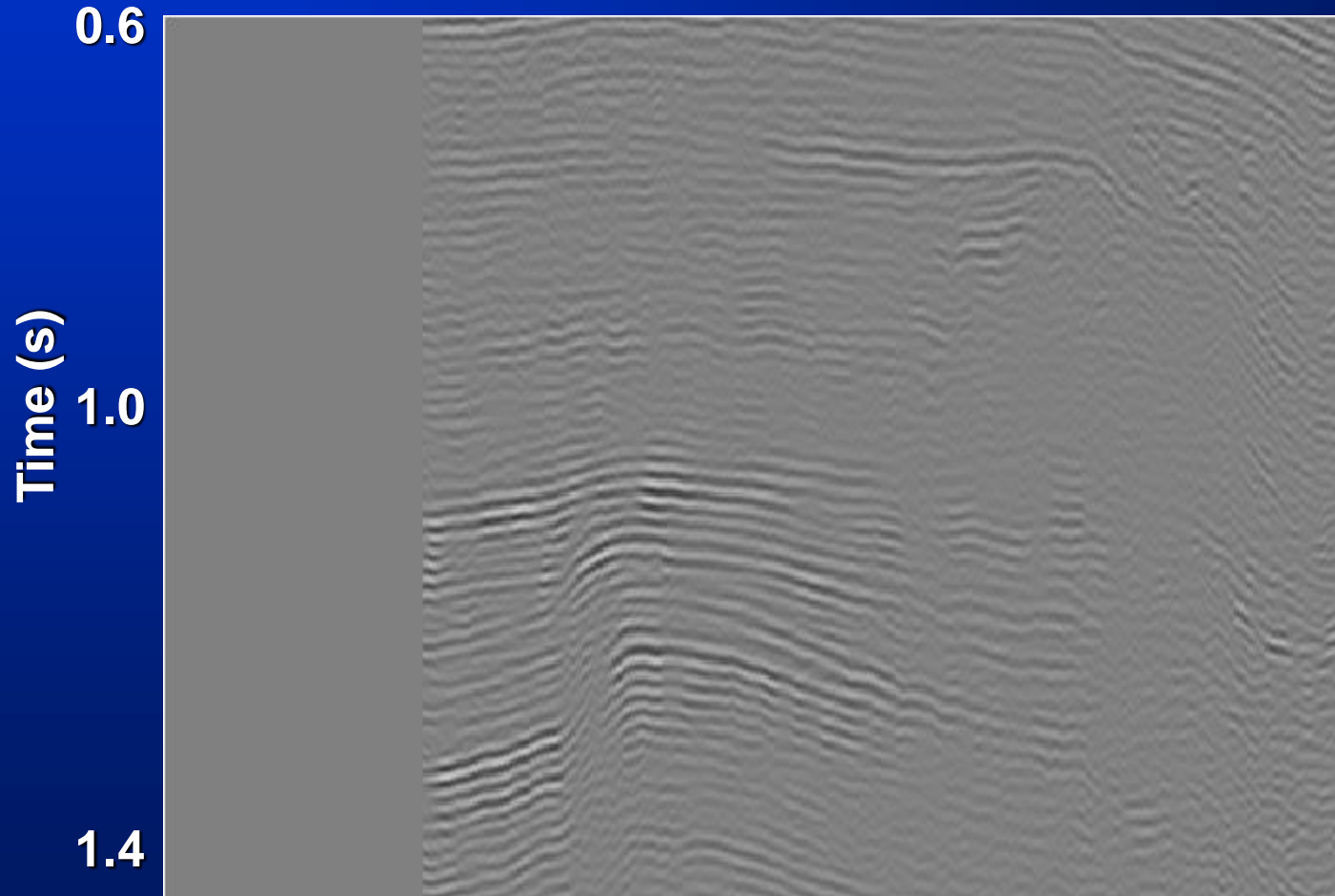
High-pass filter ($f_{low}=40$ Hz)



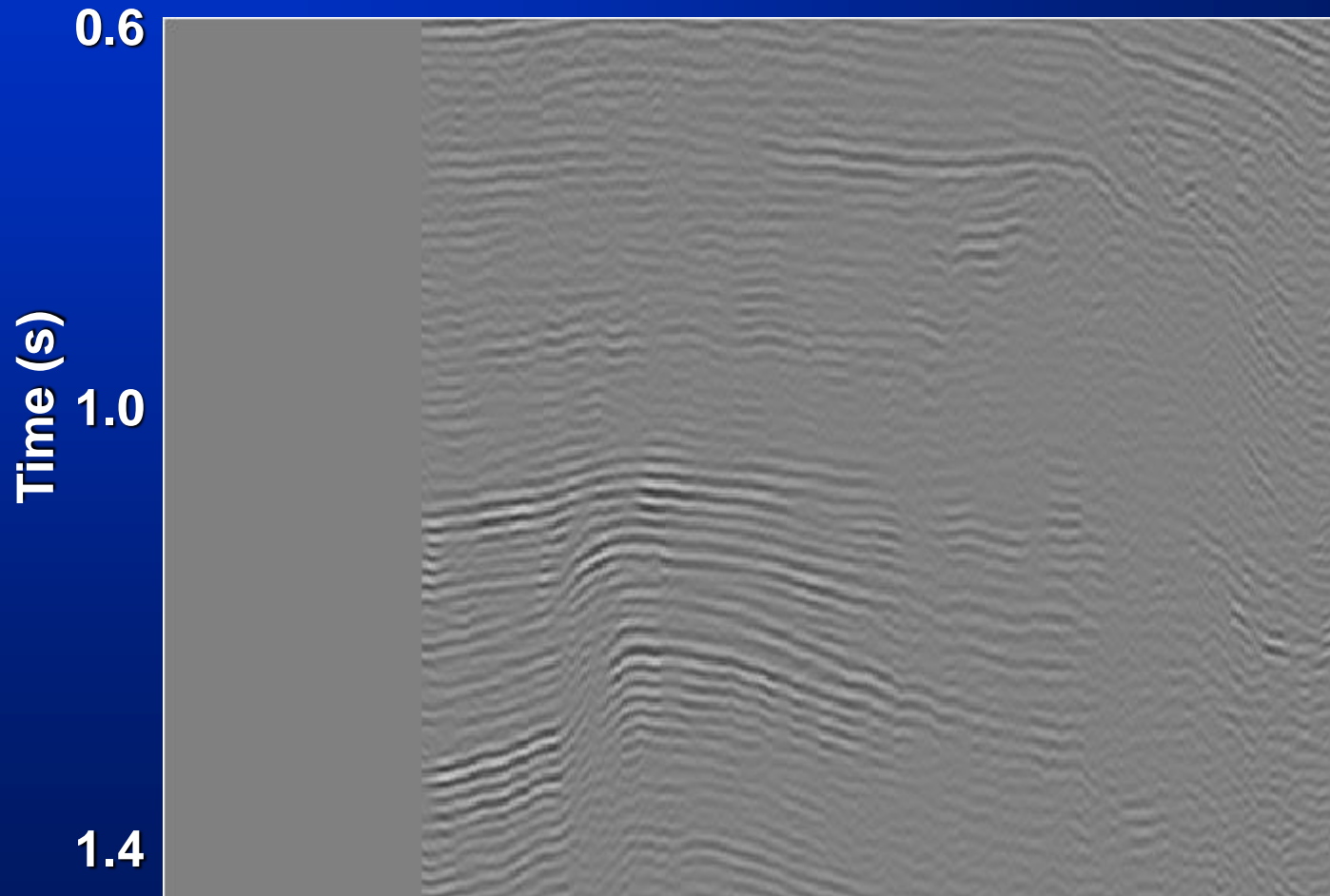
High-pass filter ($f_{low}=50$ Hz)



High-pass filter ($f_{low}=60$ Hz)



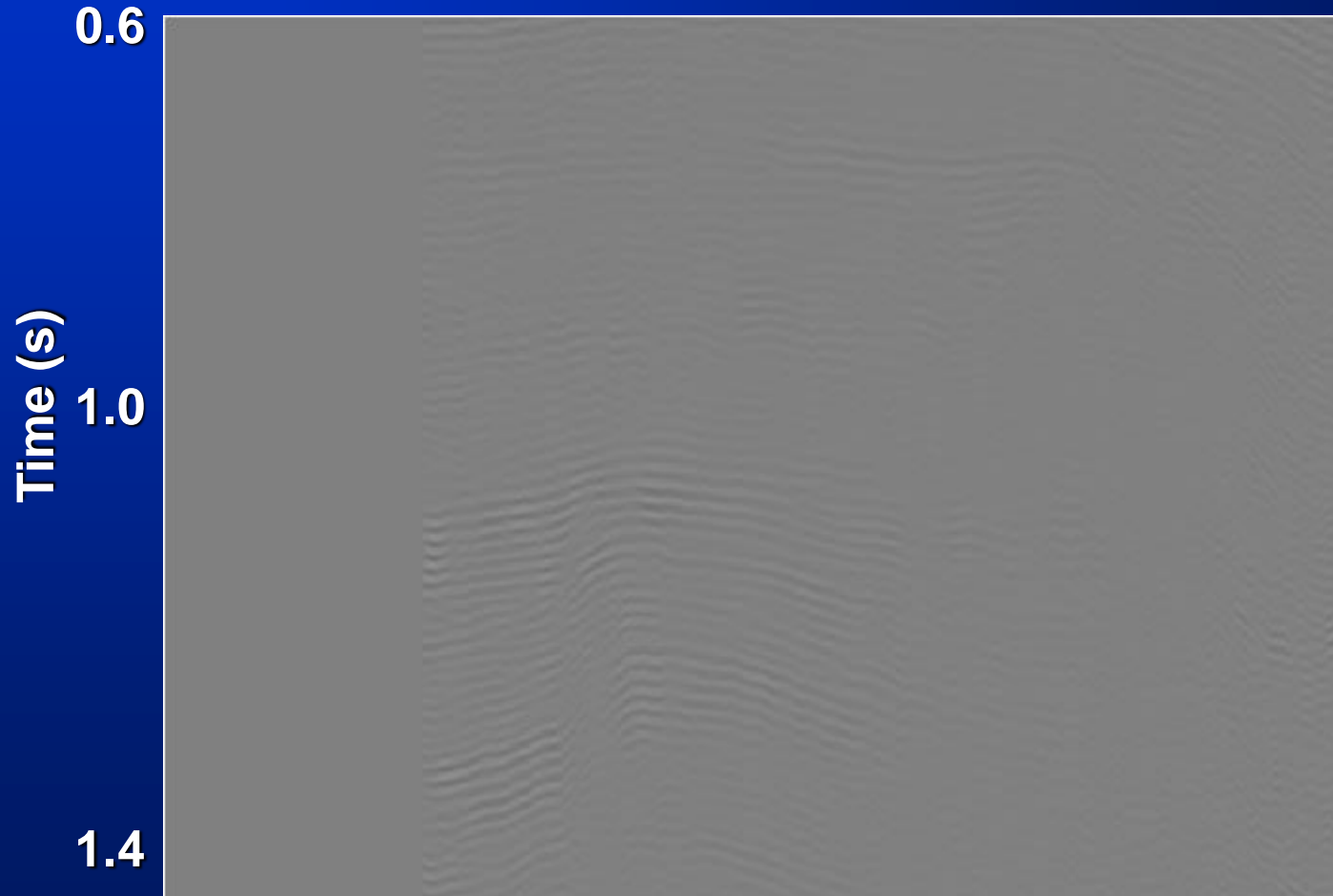
High-pass filter ($f_{\text{low}}=70$ Hz)



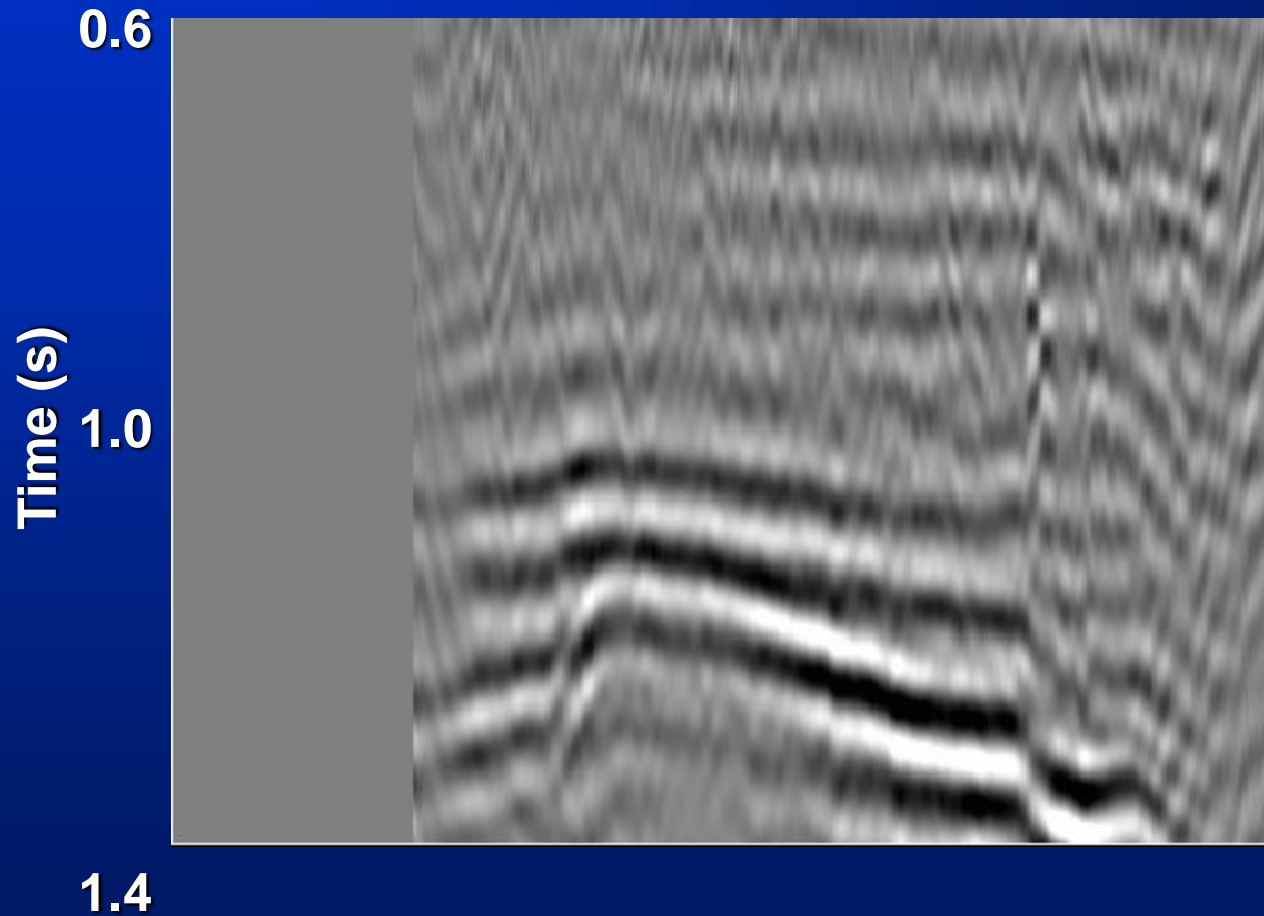
High-pass filter ($f_{low}=80$ Hz)



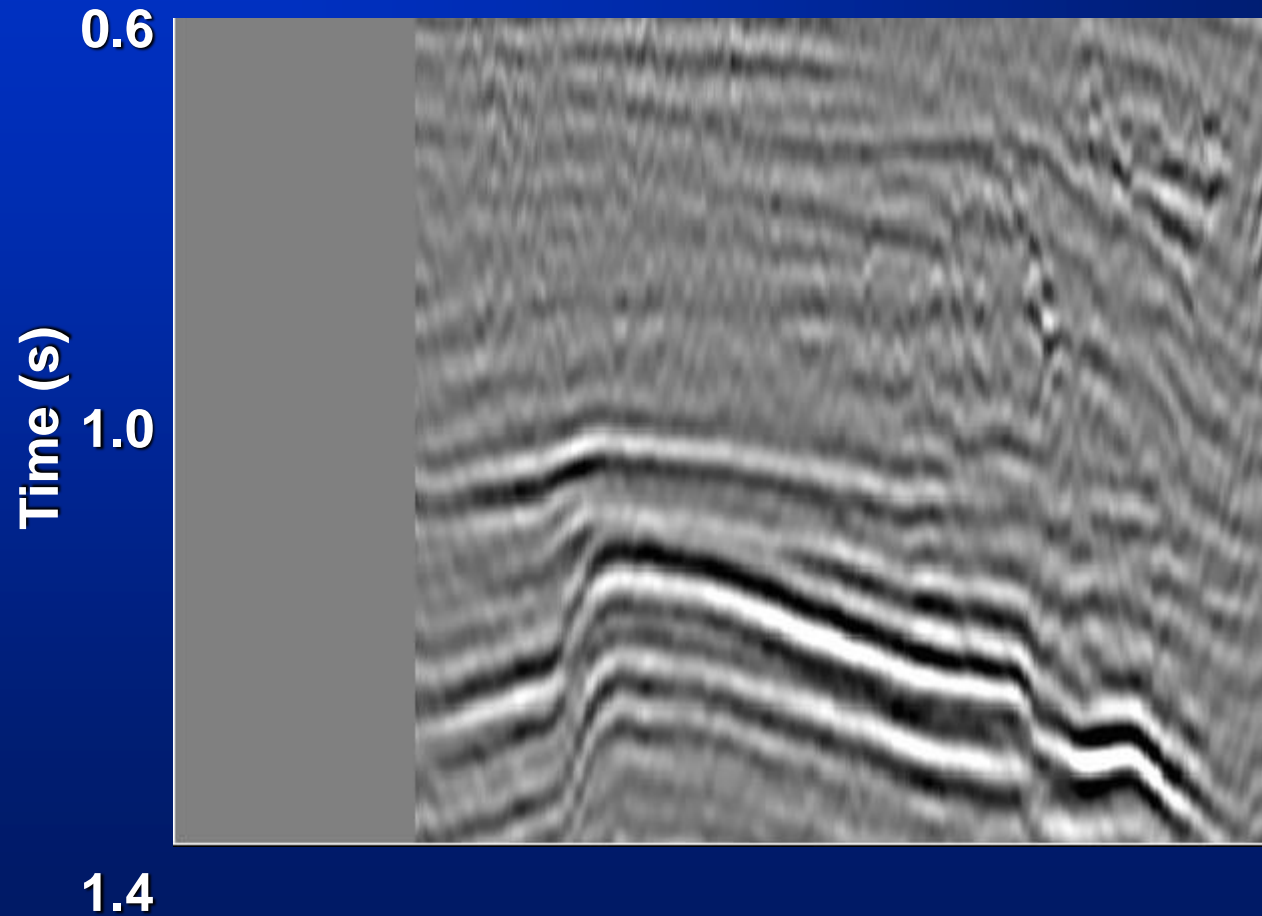
High-pass filter ($f_{low}=90$ Hz)



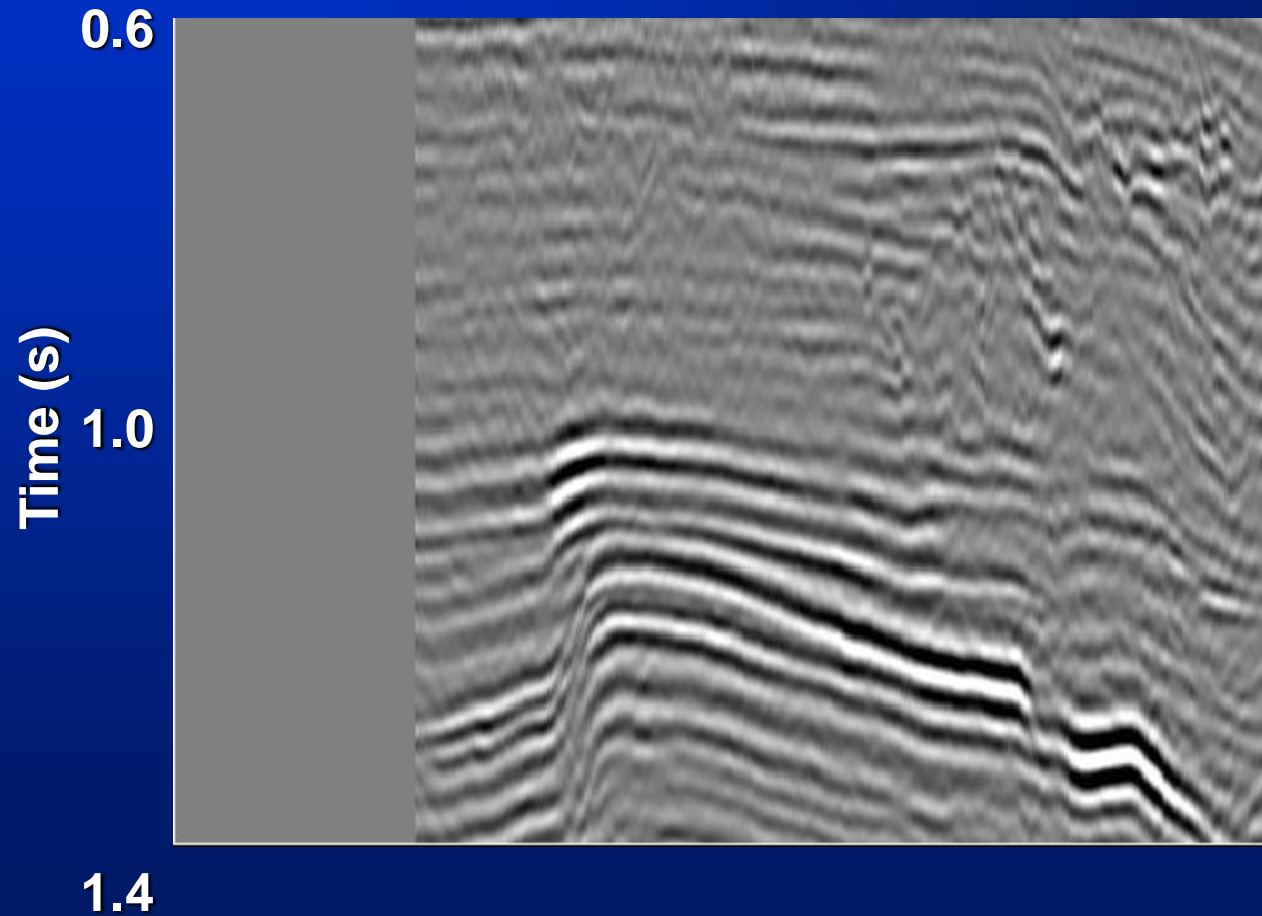
Band-pass filter (0-10 Hz)



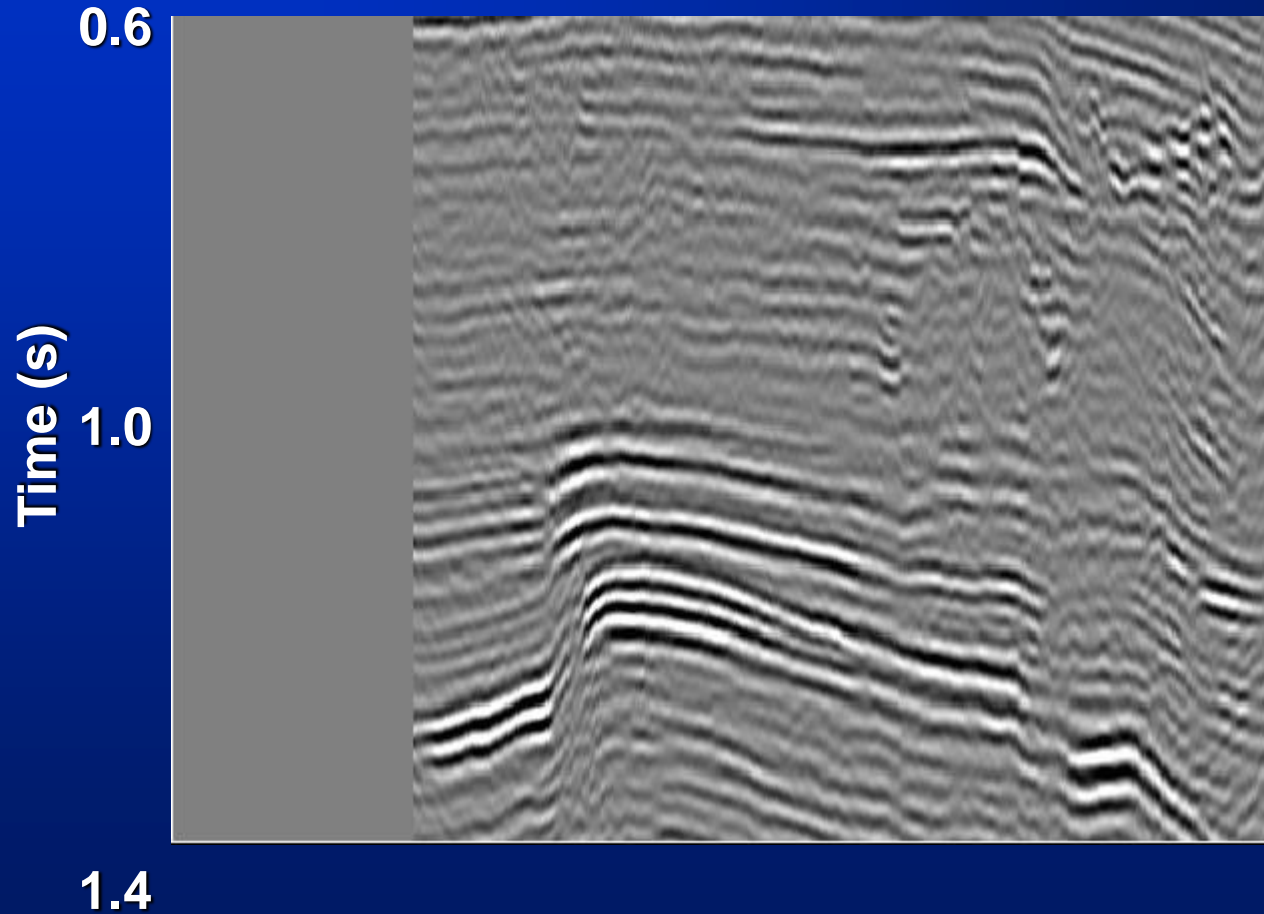
Band-pass filter (10-20 Hz)



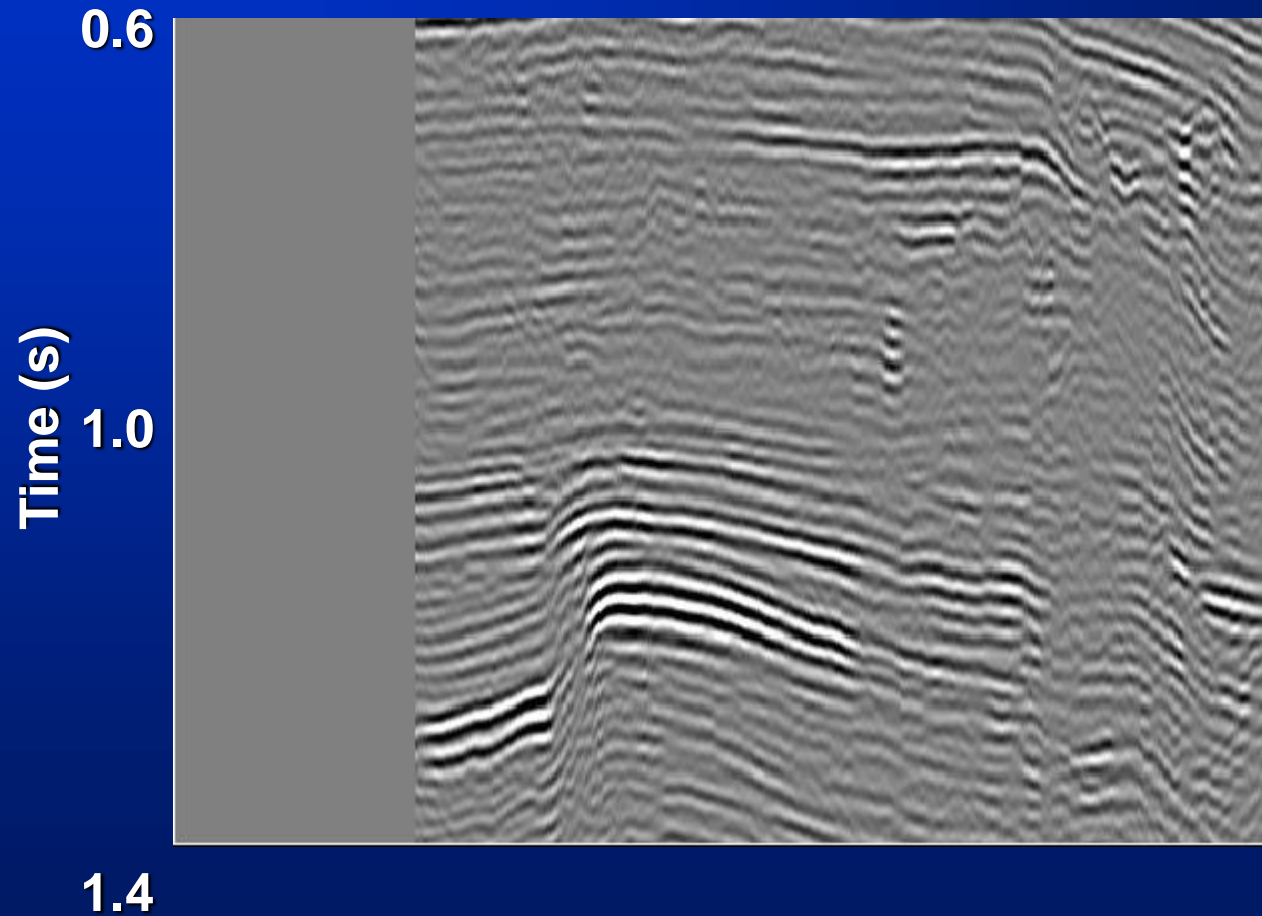
Band-pass filter (30-40 Hz)



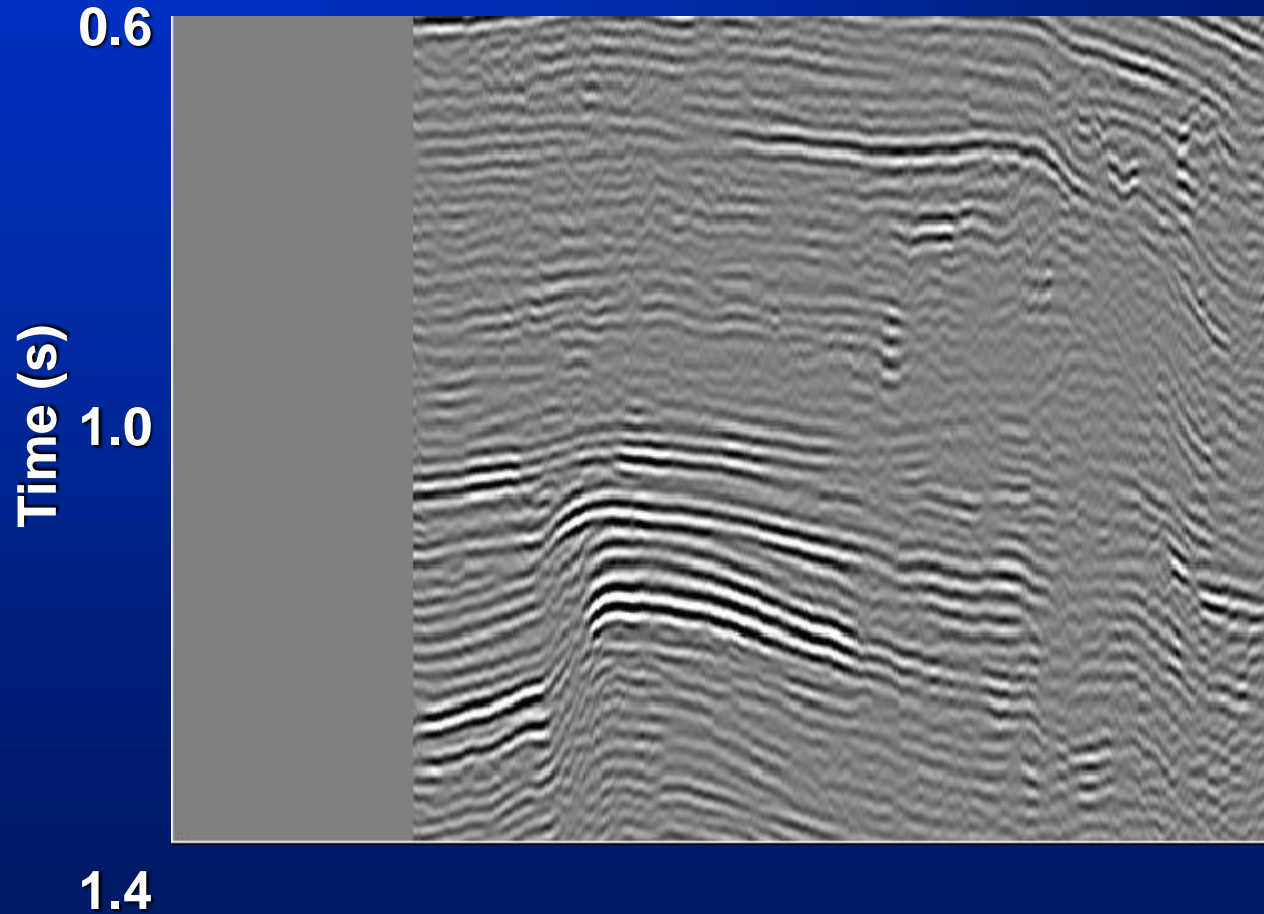
Band-pass filter (40-50 Hz)



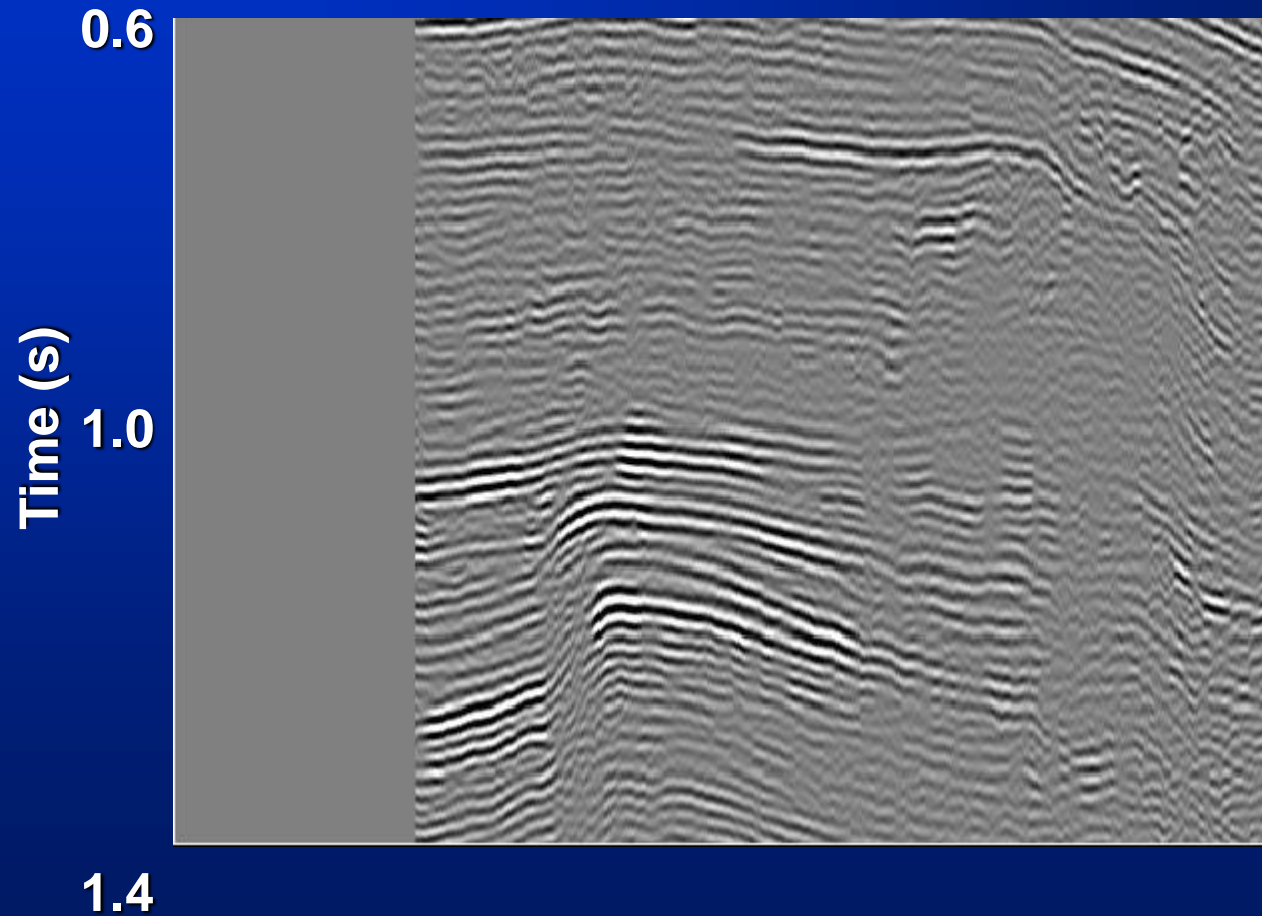
Band-pass filter (50-60 Hz)



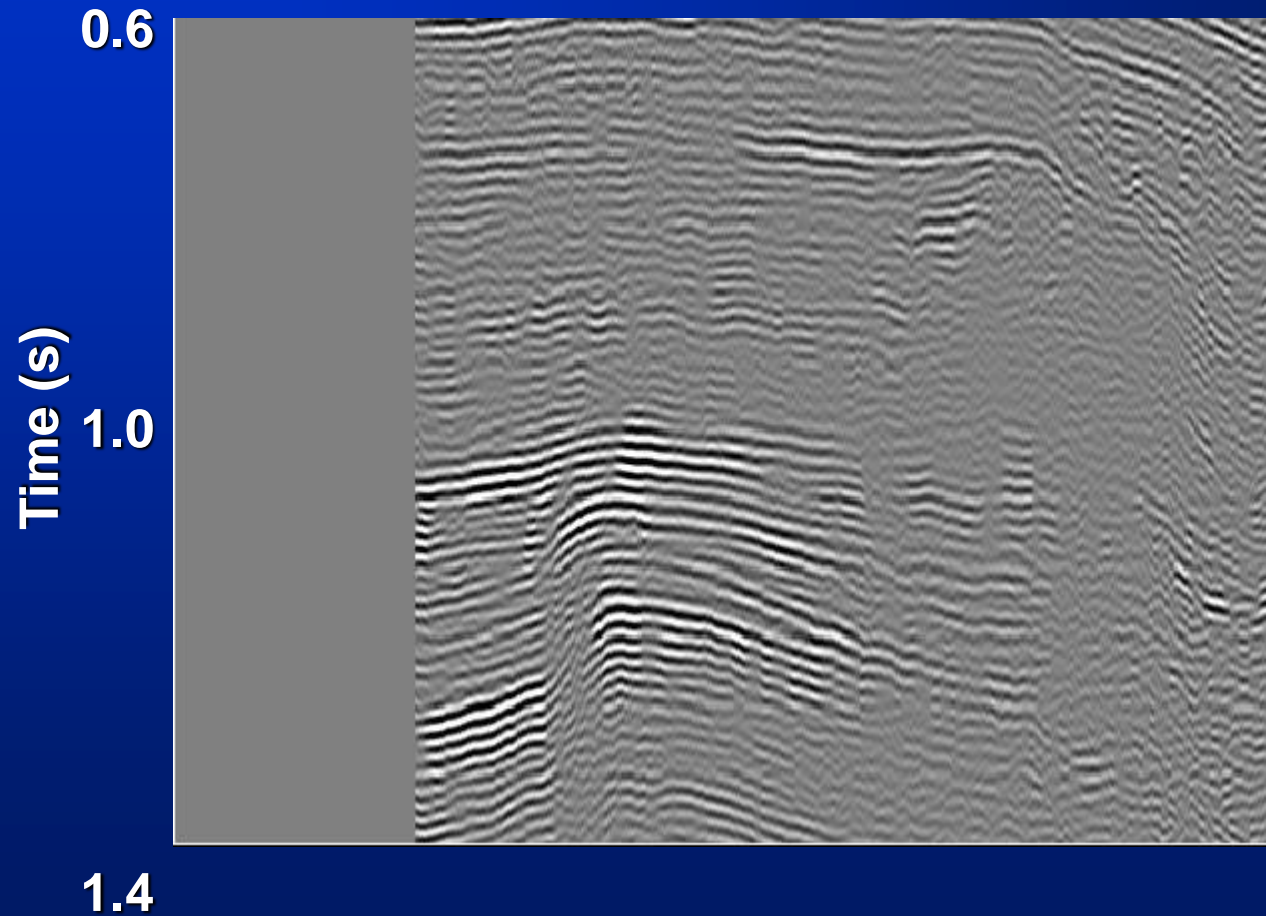
Band-pass filter (60-70 Hz)



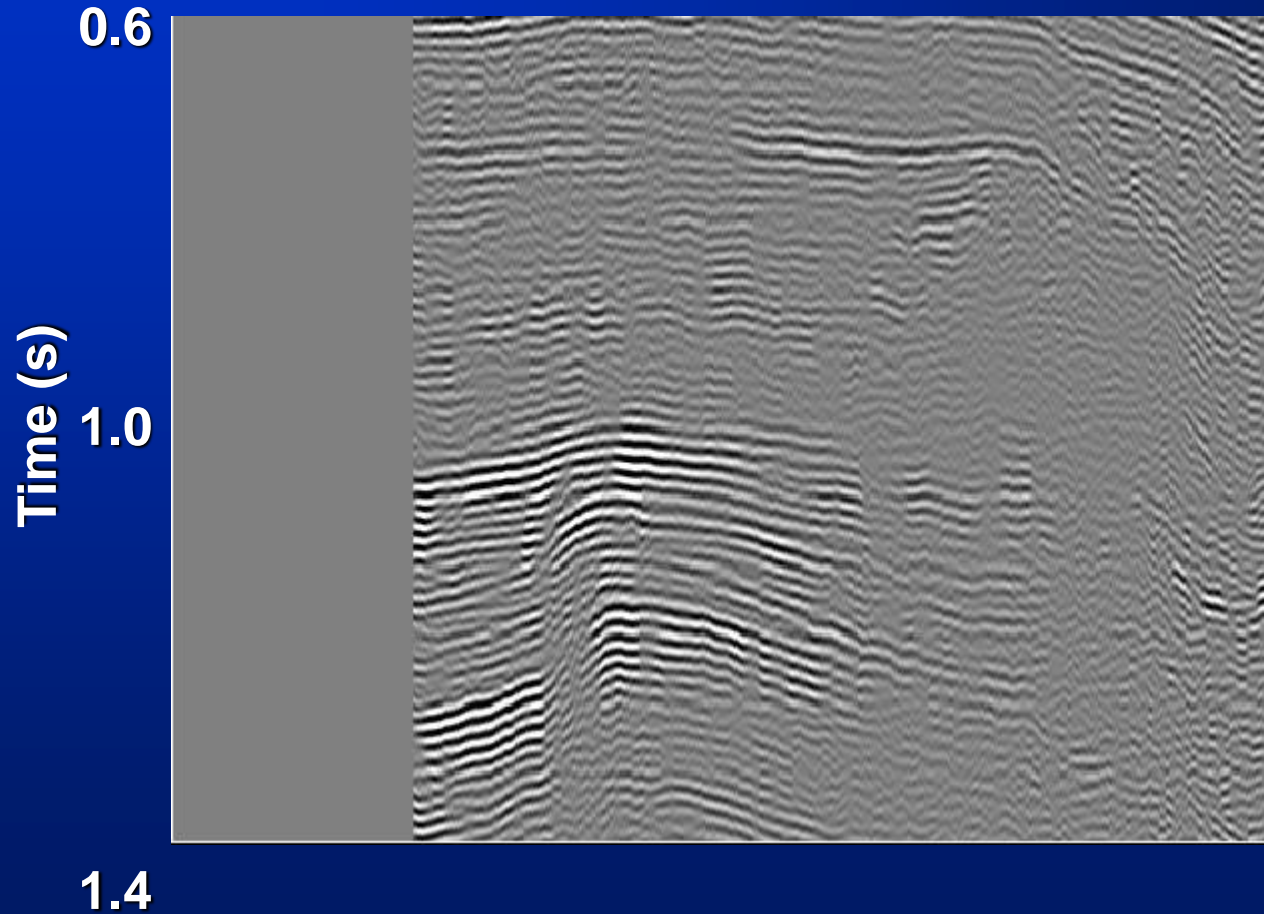
Band-pass filter (70-80 Hz)



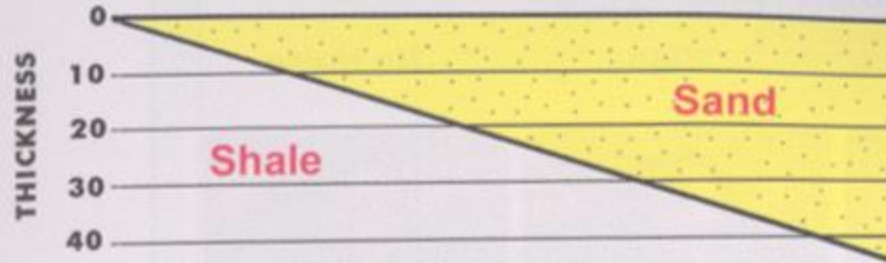
Band-pass filter (80-90 Hz)



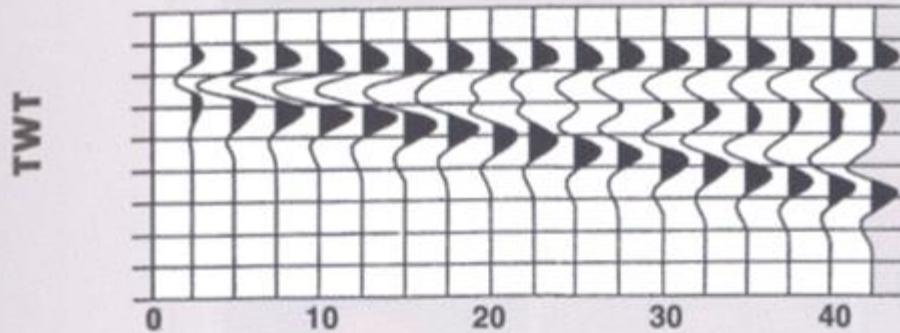
Band-pass filter (90-100 Hz)



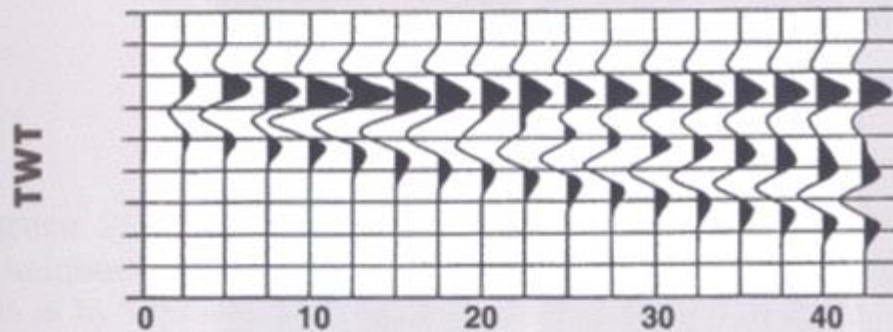
WEDGE MODEL



MINIMUM PHASE

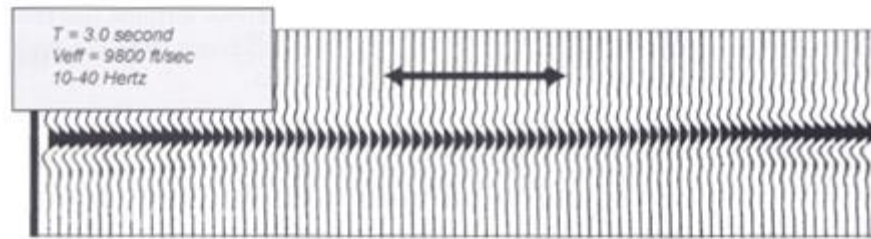
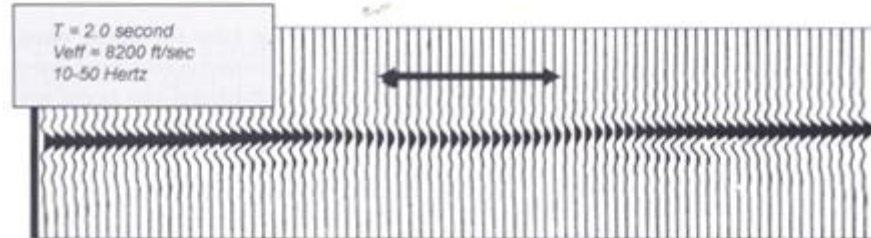
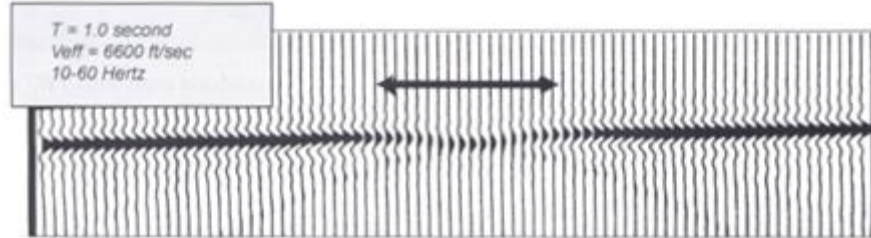
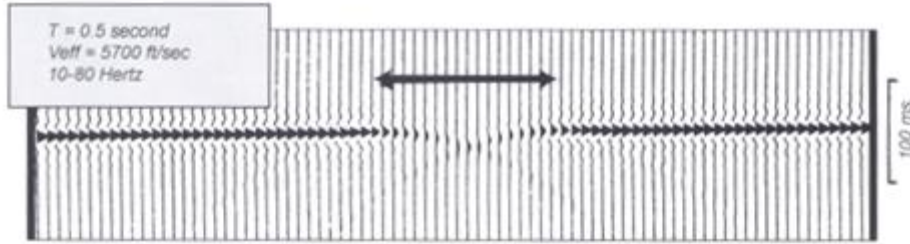


ZERO PHASE

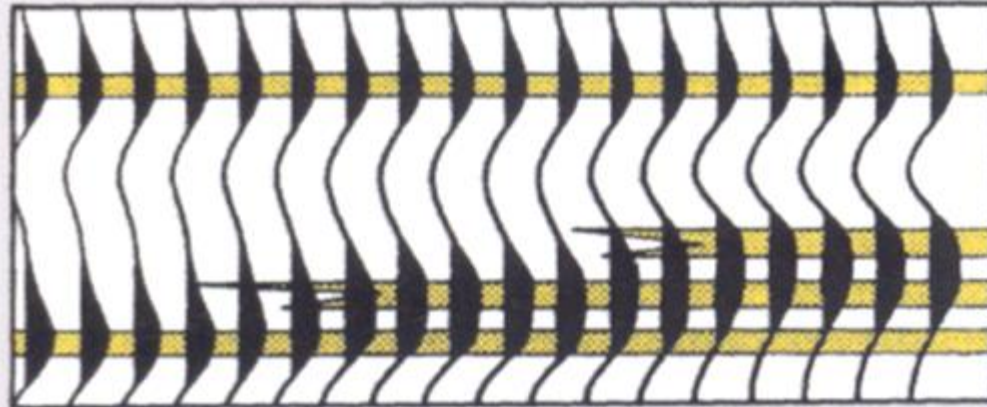


50 Hz wavelet
Period=1/50=0.020 s

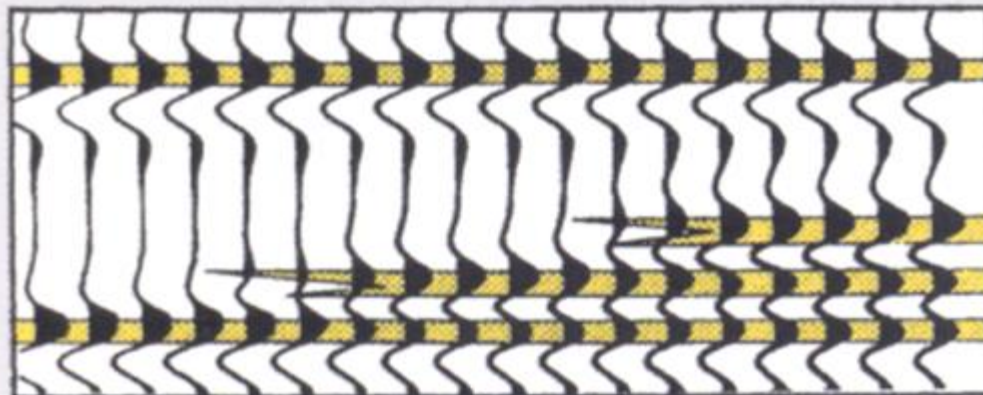
MODEL: DISCONTINUOUS REFLECTOR



Seismic response of reservoir sequence

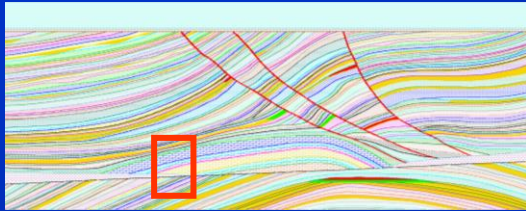


20 HERTZ PULSE



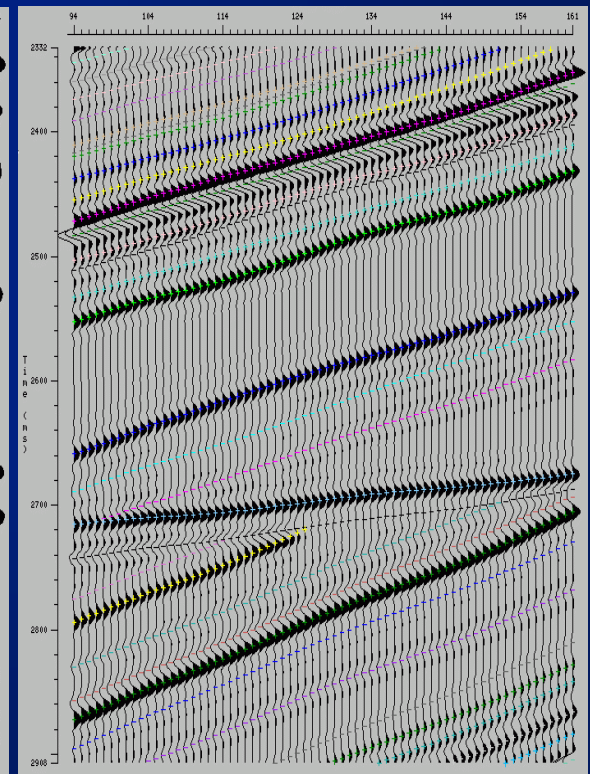
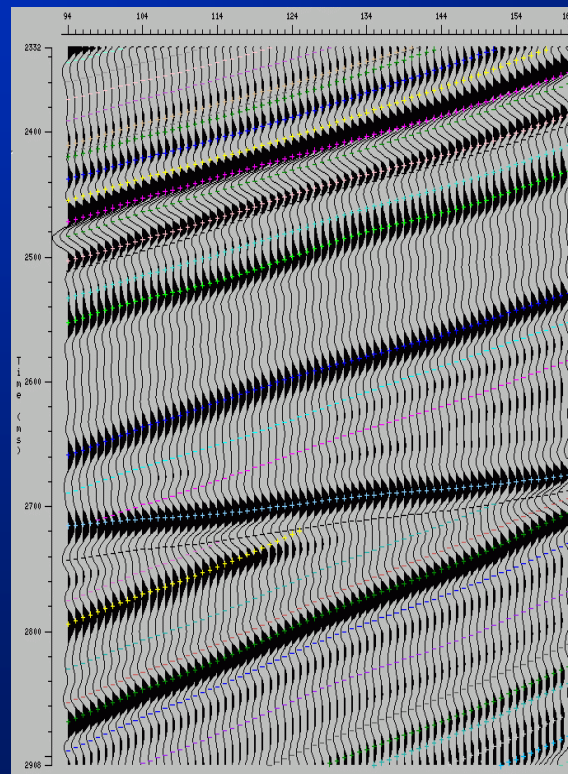
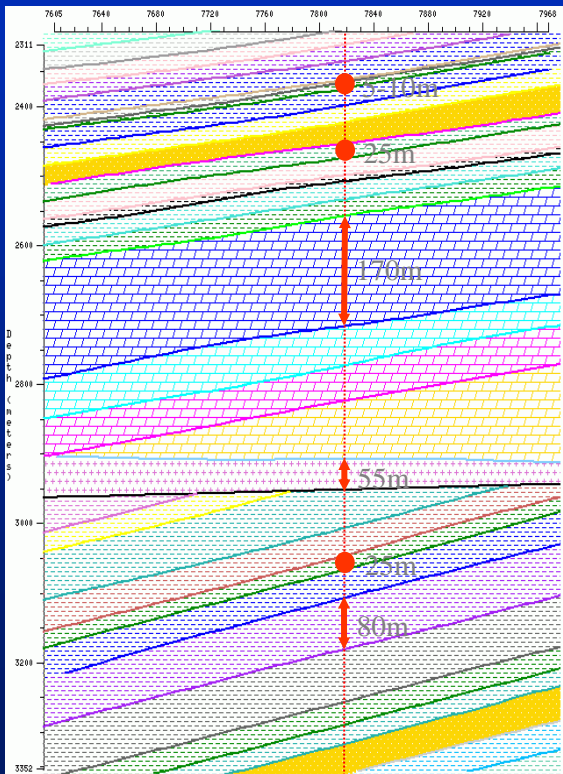
50 HERTZ PULSE

Layer Thickness and resolution



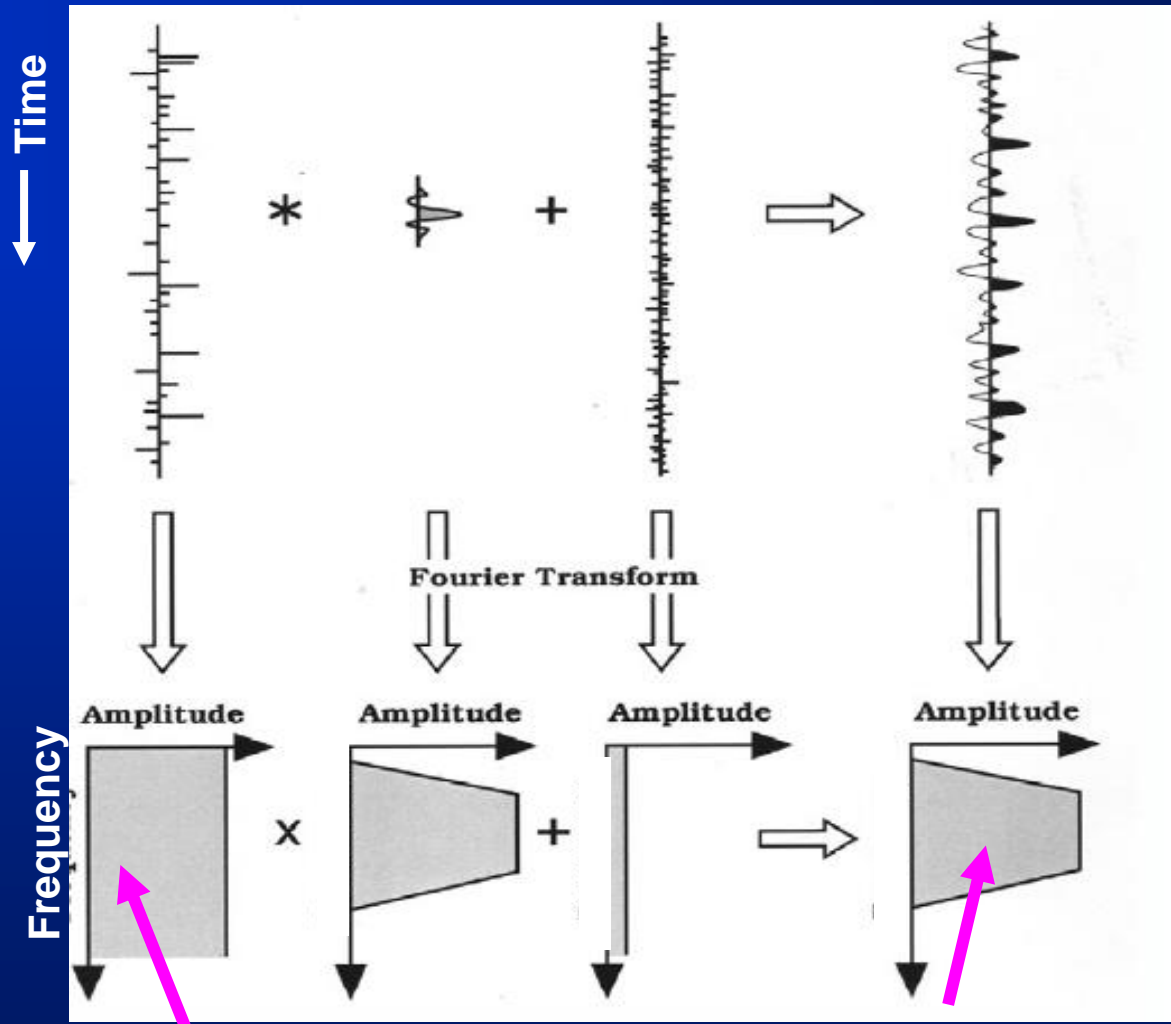
5-10-30-40 Hz

5-10-60-80 Hz



Reflectivity **Source wavelet** **Noise** **Seismic data**
 $r(t)$ $*$ $s(t)$ $+$ $n(t)$ \Rightarrow $u(t)$

**Long window
 spectral
 decomposition
 and the
 convolutional
 model**

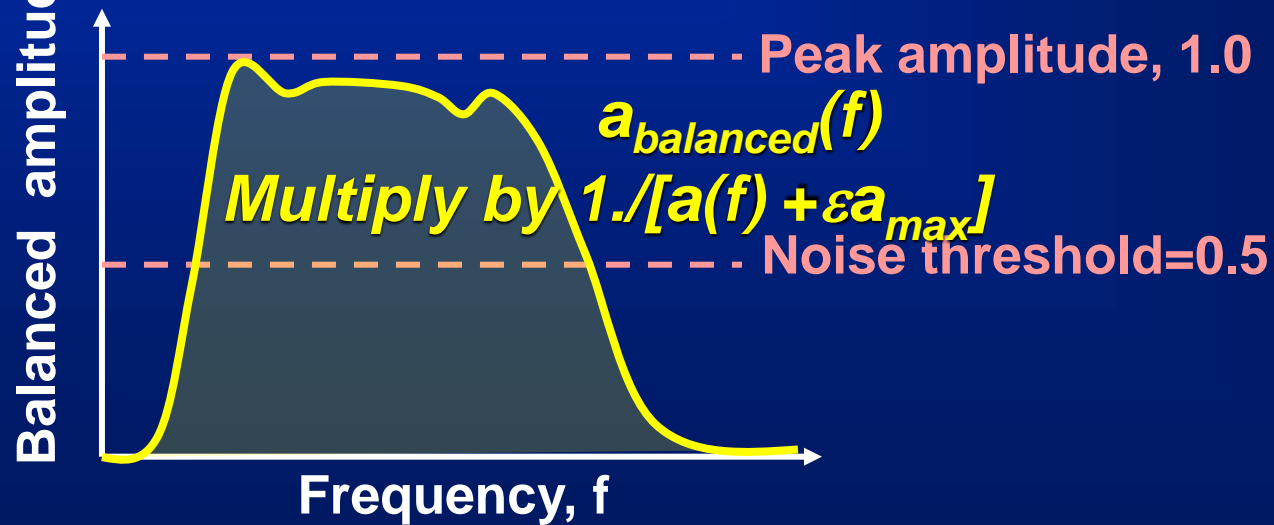
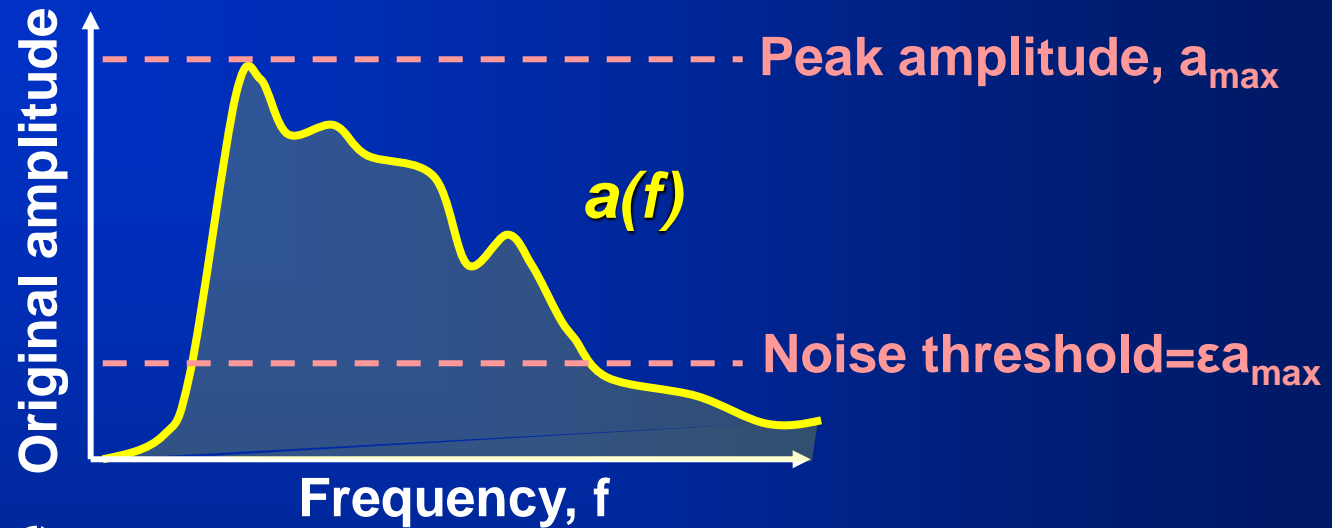


White spectrum

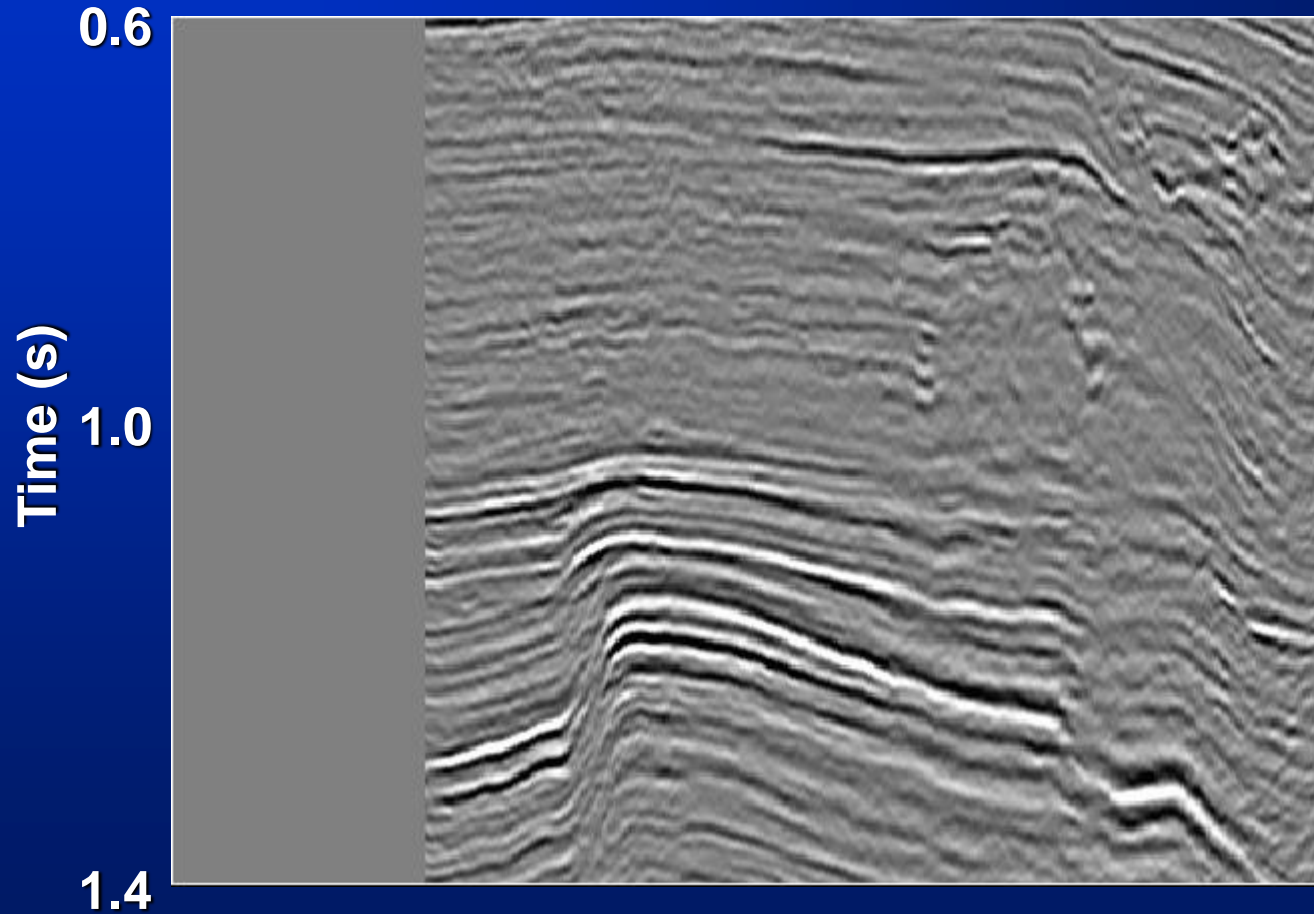
Bandlimited white spectrum

(Partyka et al, 1999)

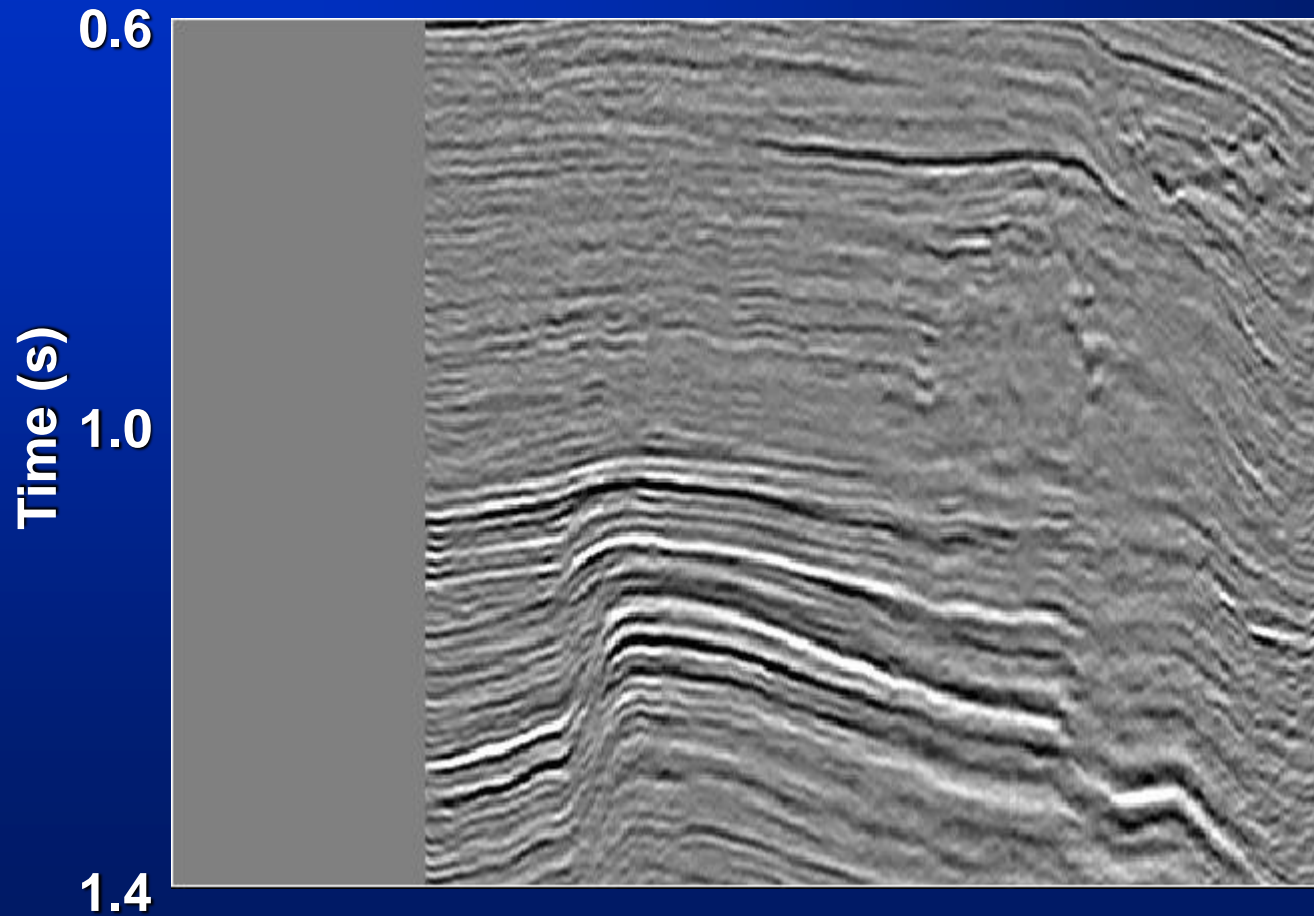
Spectral balancing

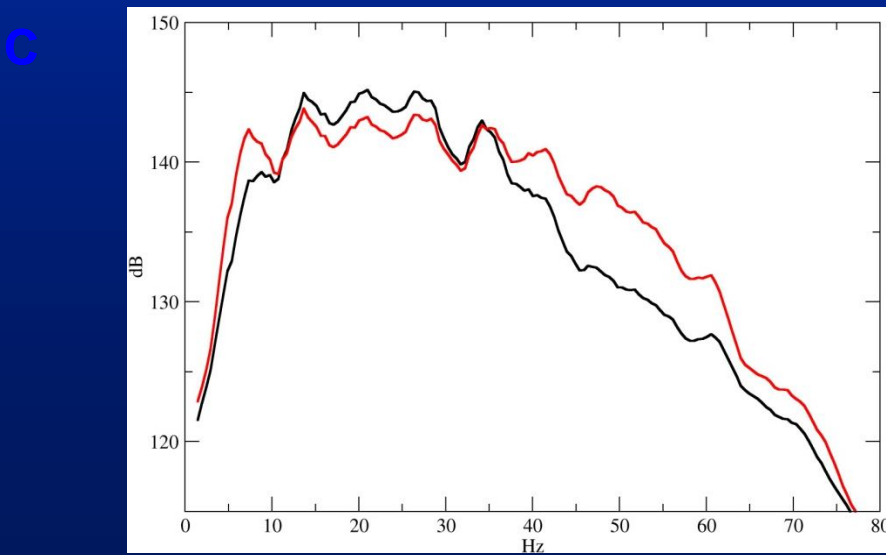
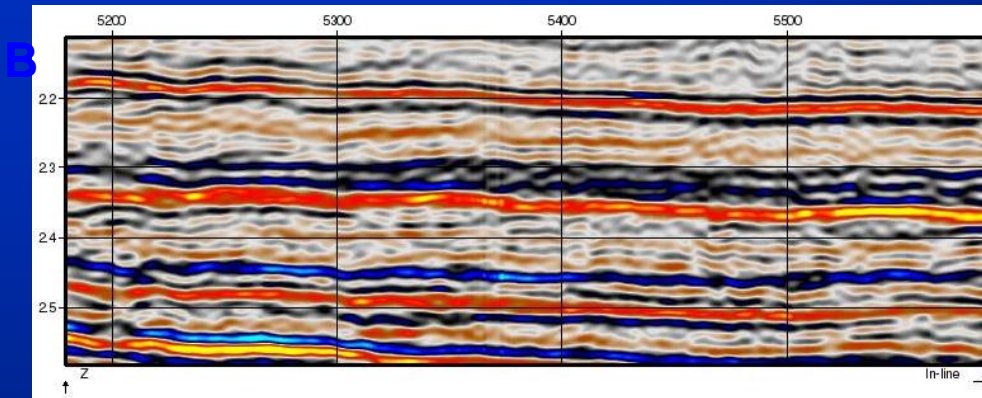
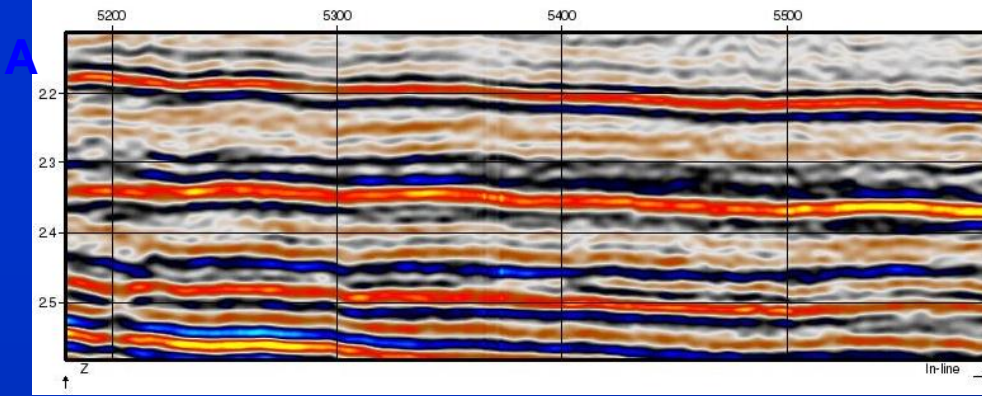


Original data (west Texas)



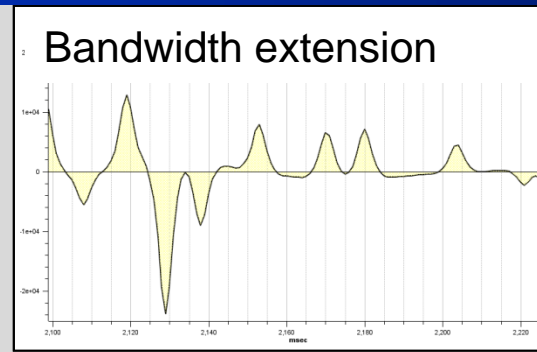
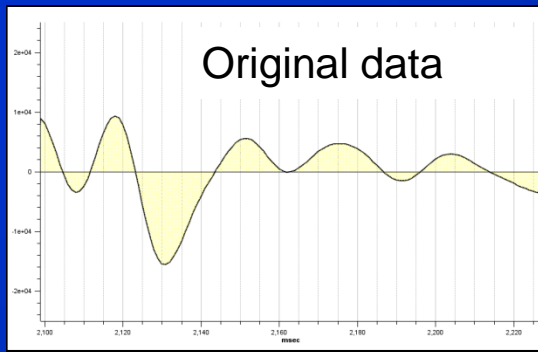
Spectrally balanced data





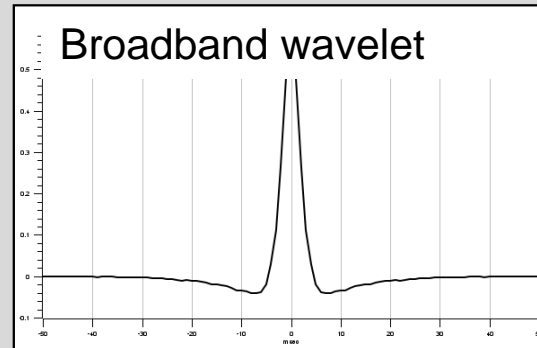
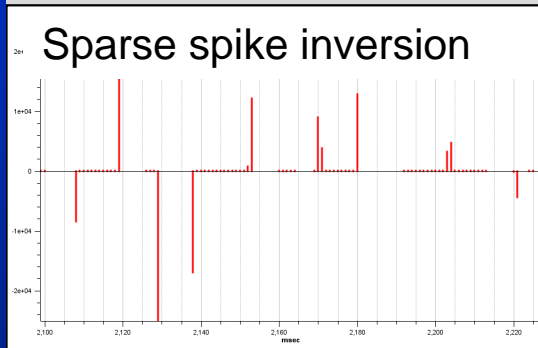
(Carrao et al., 2011)

Bandwidth Extension



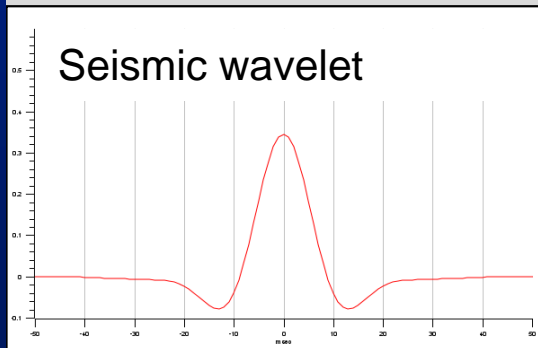
\approx

$=$



$*$

$*$



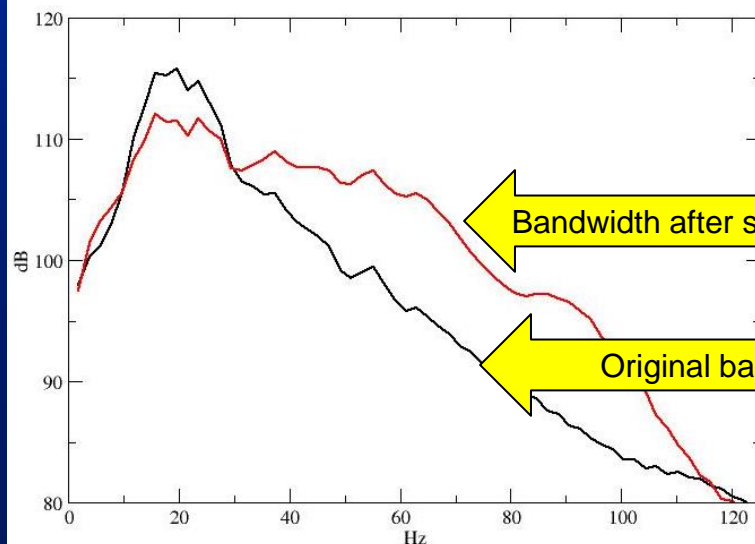
(Carrao et al., 2011)

Bandwidth Extension

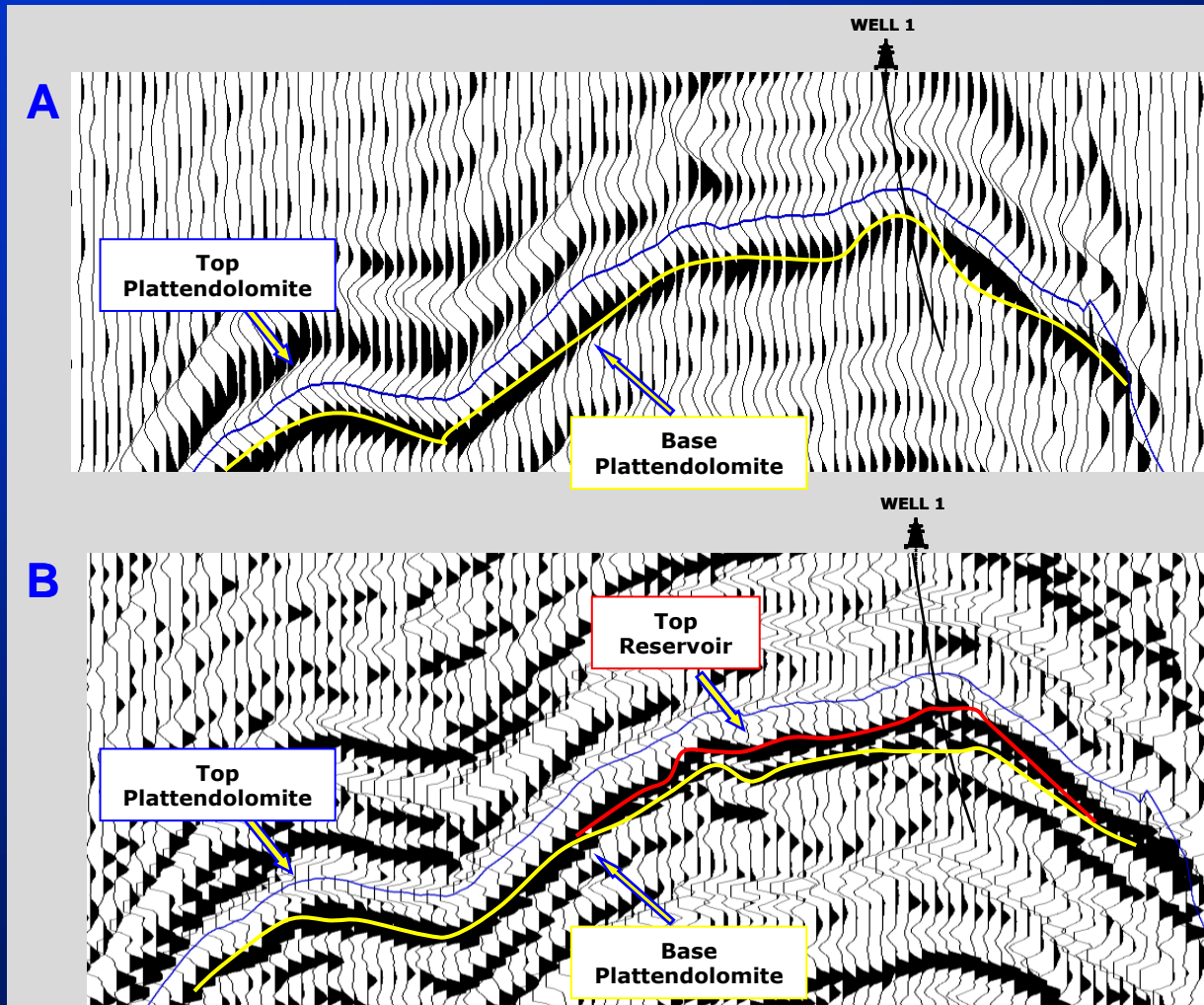
Original data

Data after sparse spike deconvolution

Warning! Always compare resulting data to well logs after bandwidth extension!



Bandwidth Extension

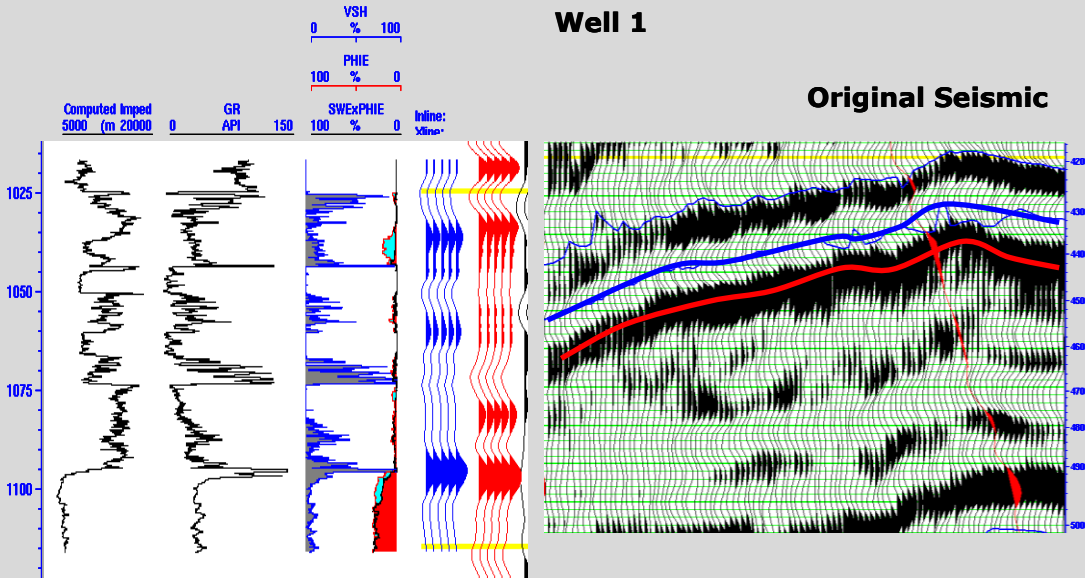


Original data

Data after sparse
spike
deconvolution

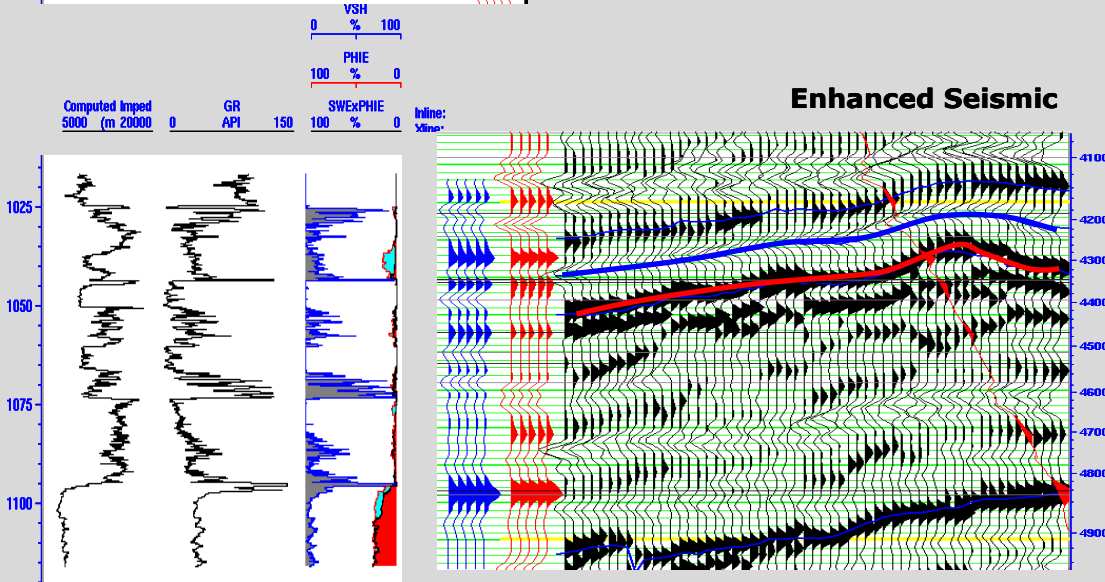
Bandwidth Extension: Check well ties!

A



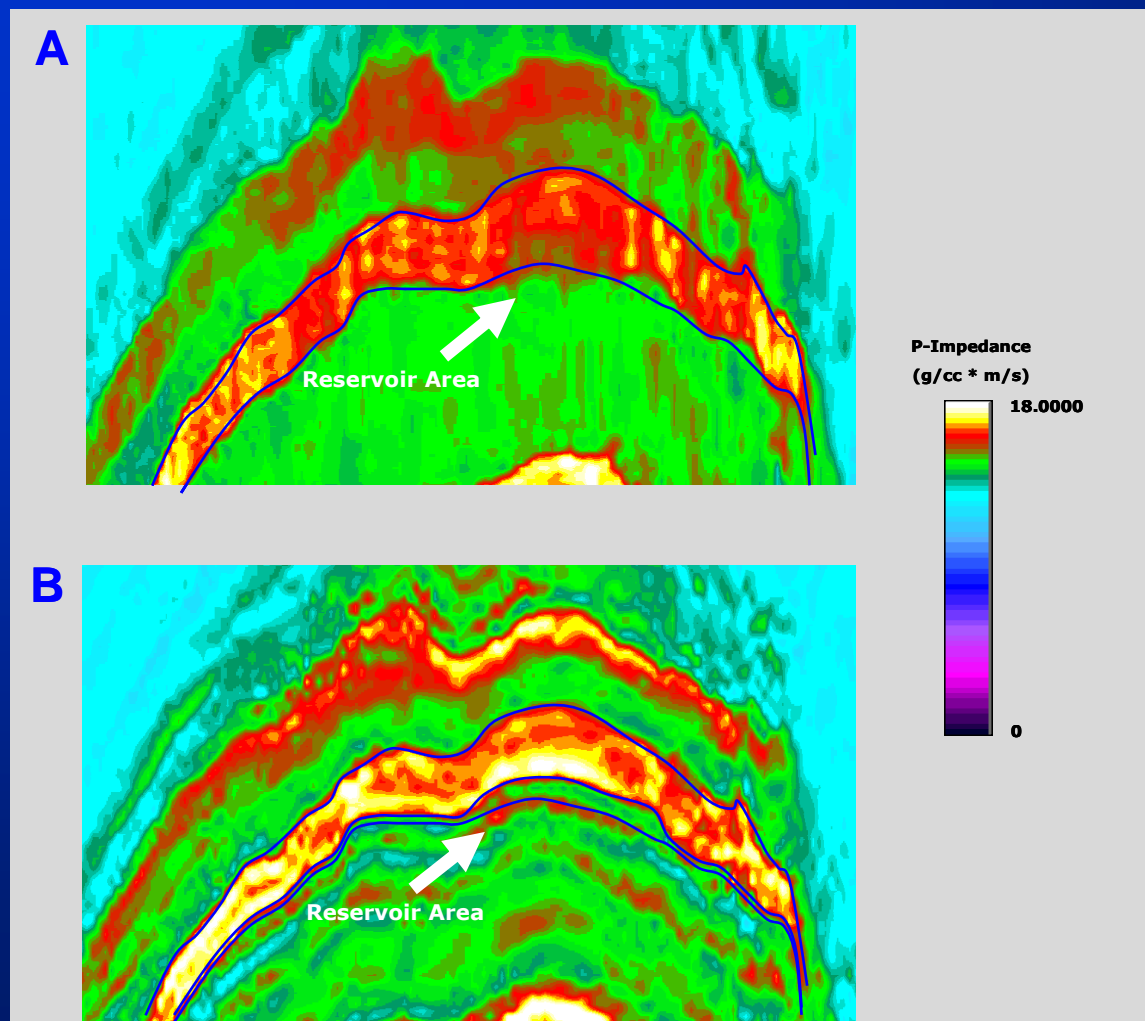
Original data

B



Data after sparse spike deconvolution

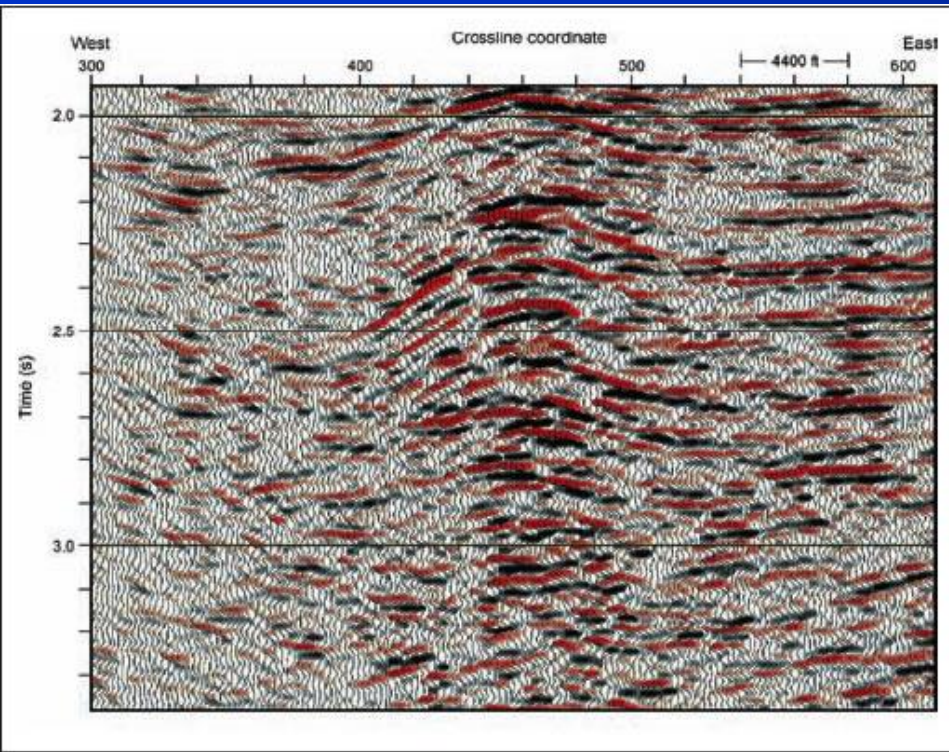
Bandwidth Extension: Influence on impedance inversion



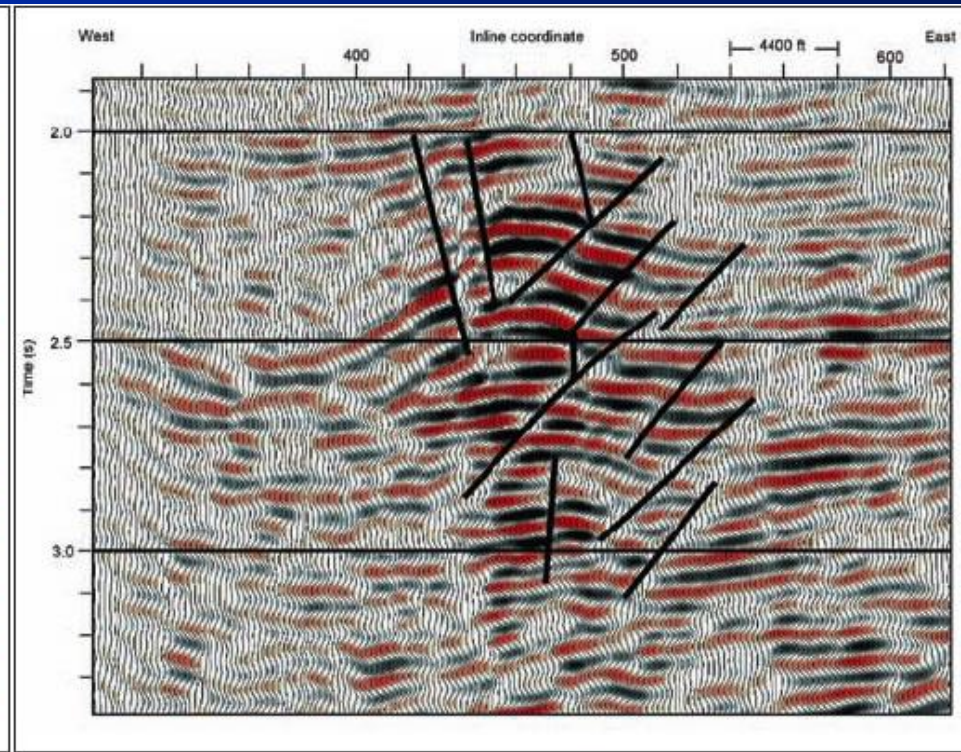
Original data

Data after sparse
spike
deconvolution

Improving interpretability by throwing away data

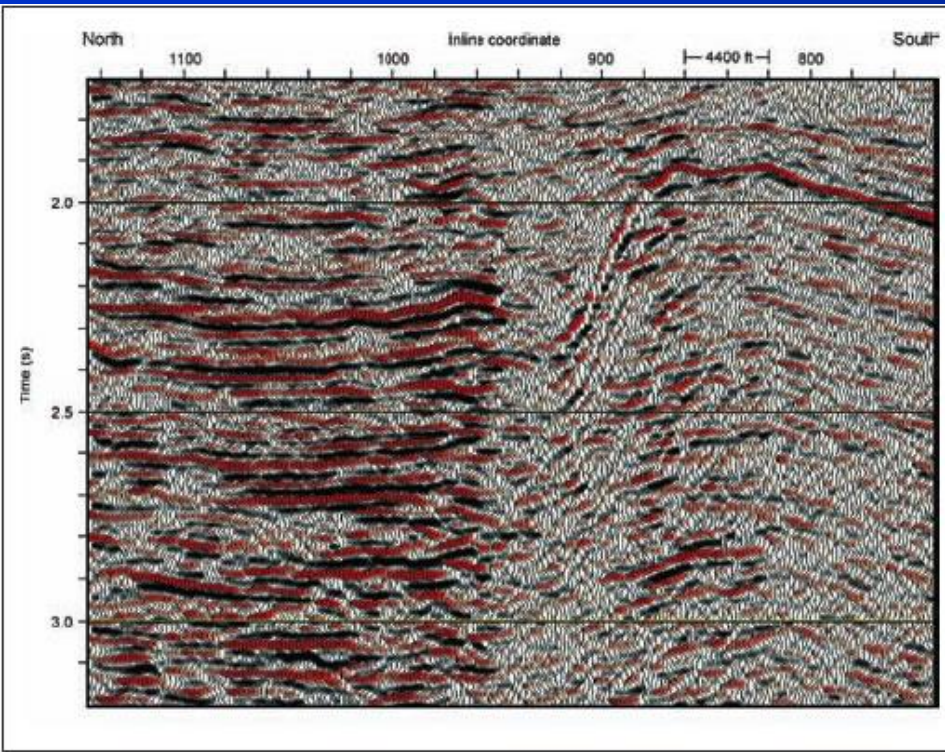


Poor statics negatively impact the high frequencies in this broad band 8-80 Hz data

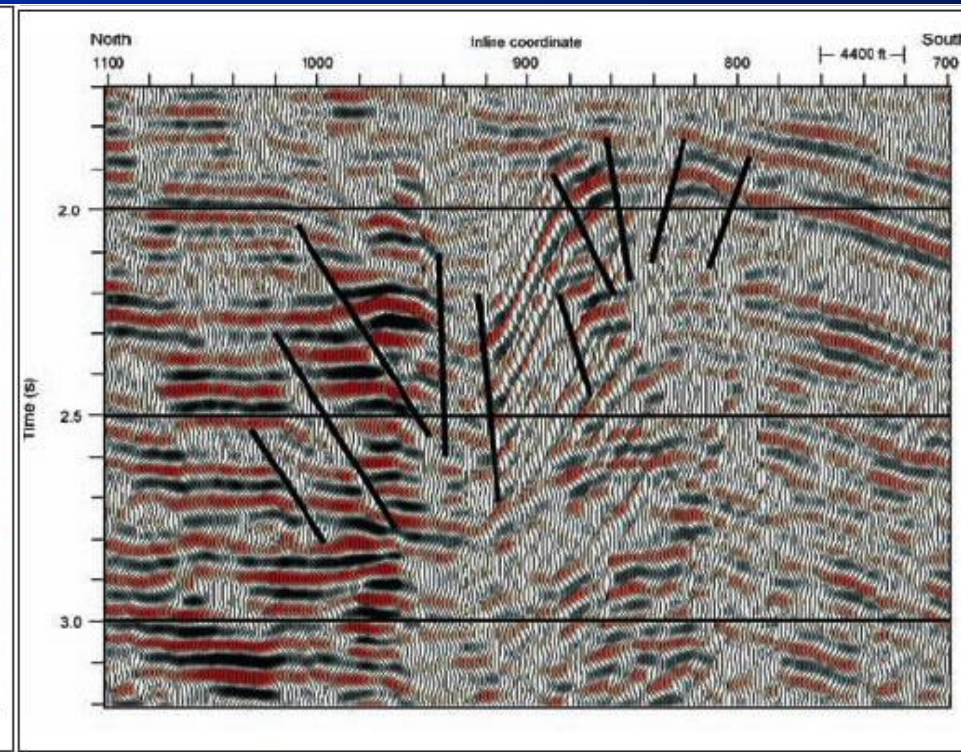


Data filtered back to 8-16 Hz (low frequencies less impacted by poor statics)

Improving interpretability by throwing away data



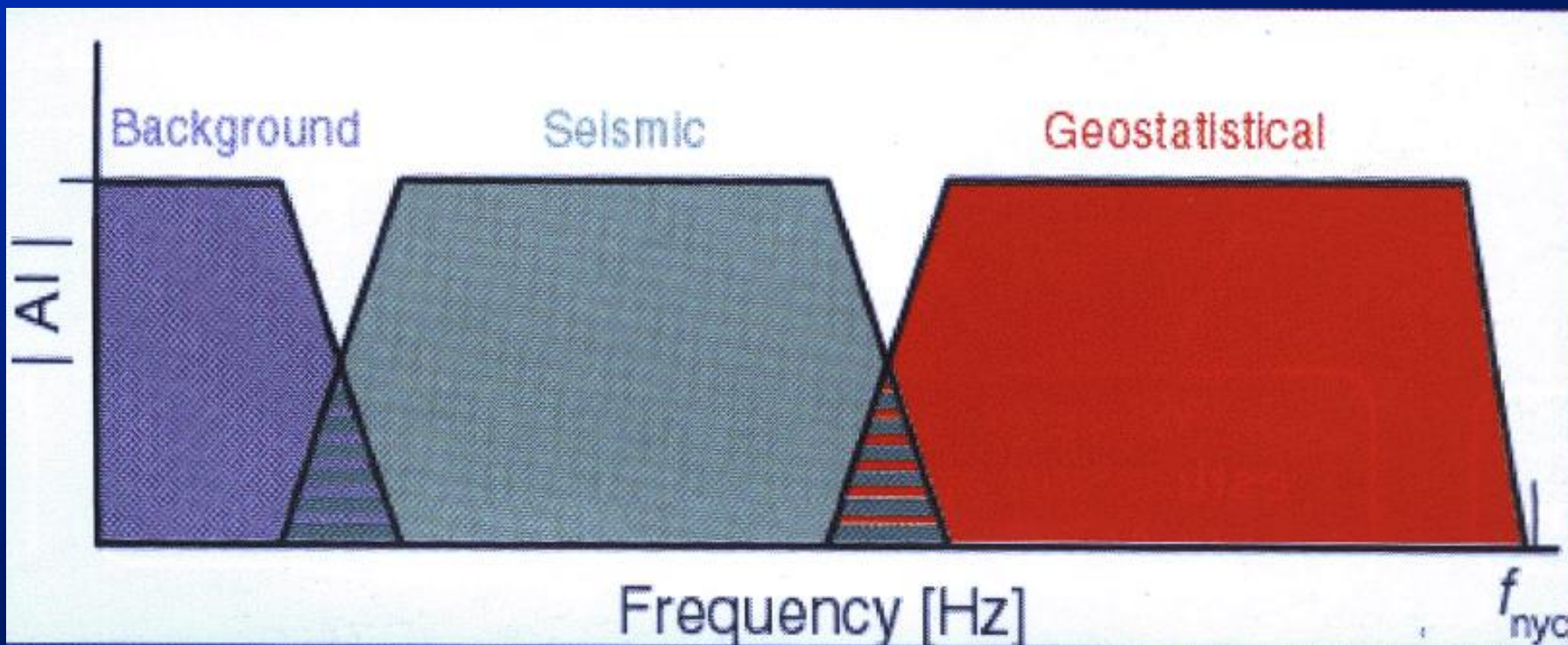
Poor statics negatively impact the high frequencies in this broad band 8-80 Hz data



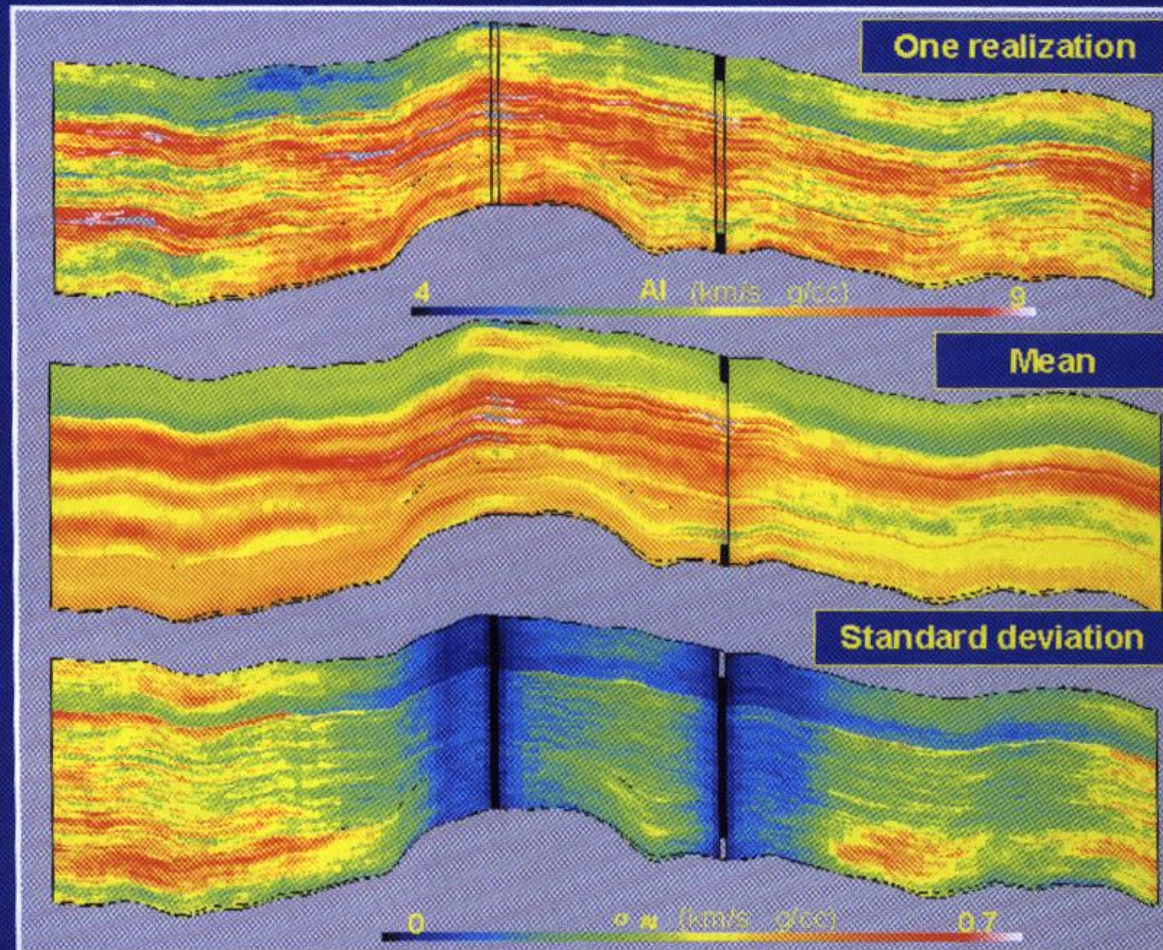
Data filtered back to 8-16 Hz (low frequencies less impacted by poor statics)

Seismic bandwidth and resolution

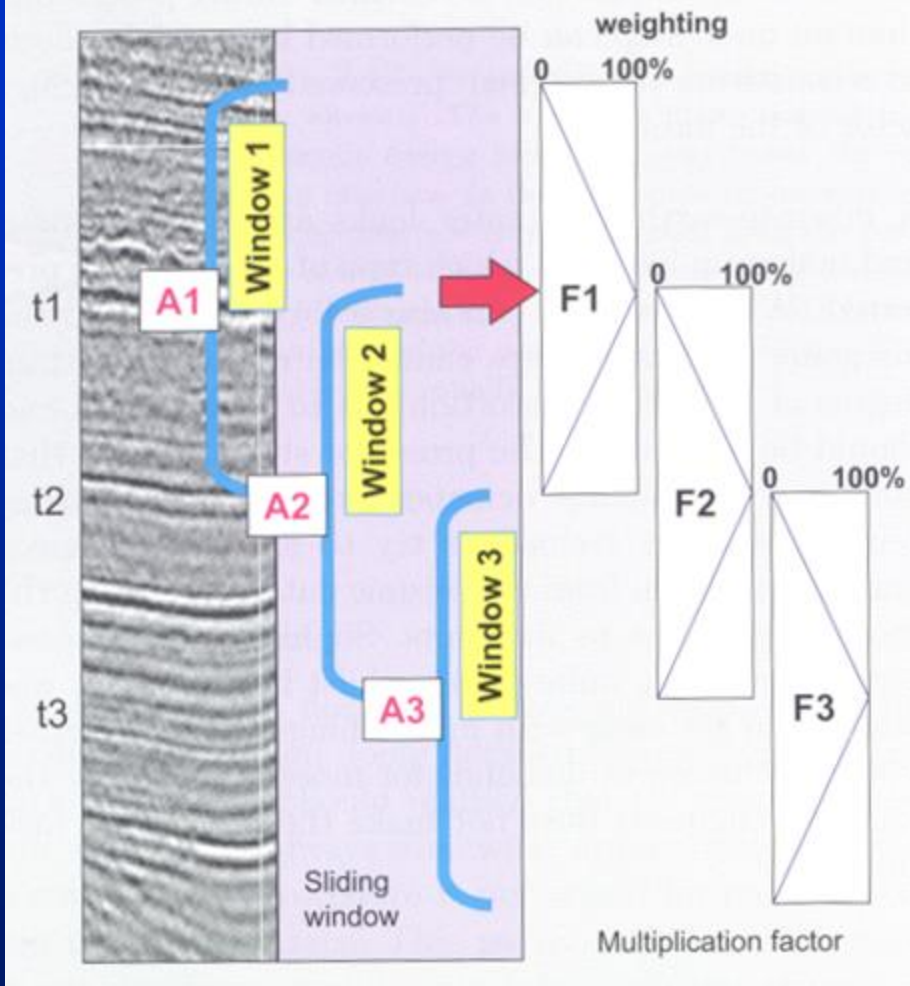
- We obtain low frequencies (< 5 Hz) from horizon interpretation, velocity analysis, and well logs
- We obtain medium frequencies (5-100 Hz) from seismic waveforms (amplitude data)
- We obtain high frequencies (> 150 Hz) from integrating well control using geostatistics or neural networks



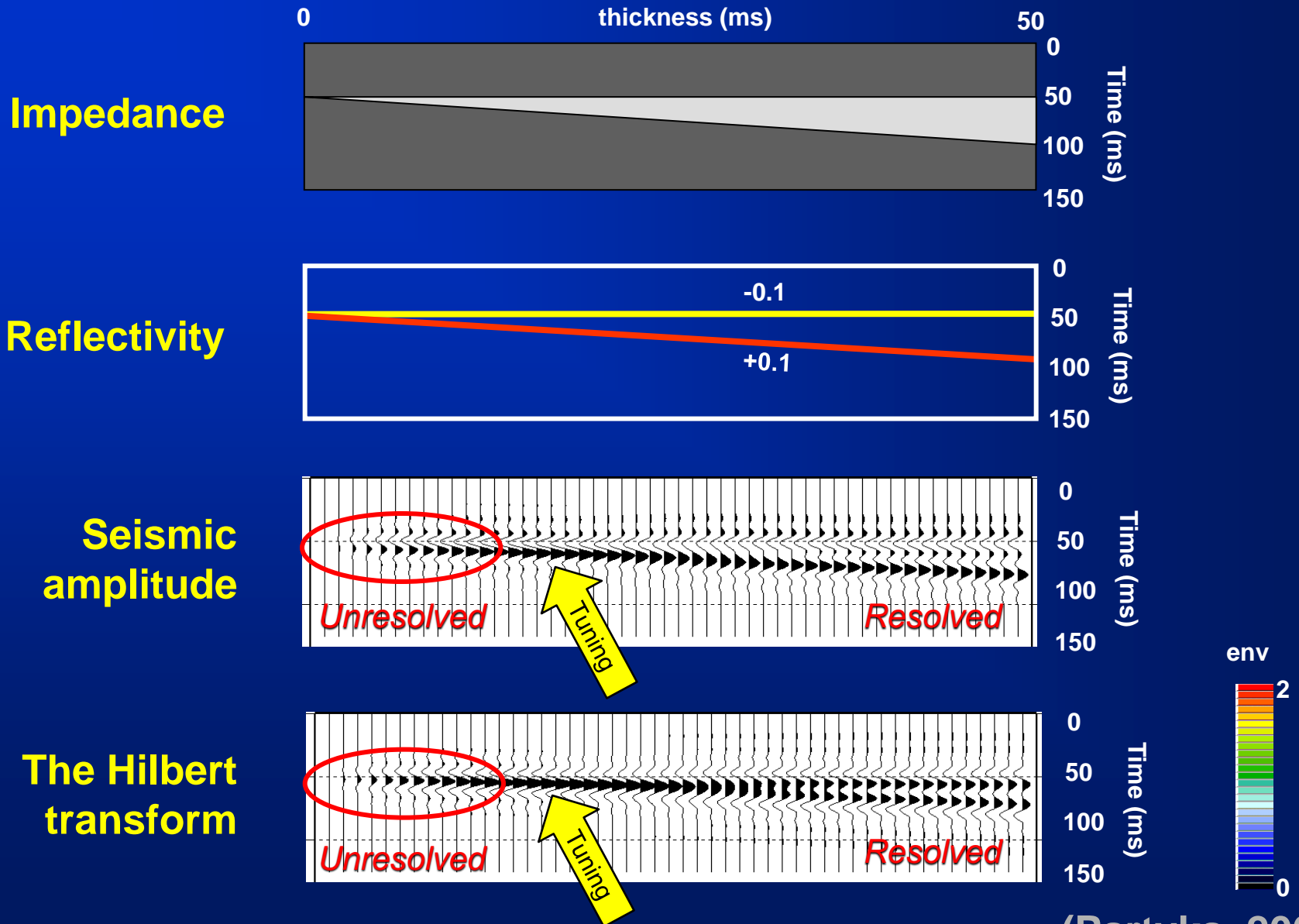
EXAMPLE OF GEOSTATISTICAL INVERSION RESULTS (LAMY ET AL., 1999)



Automatic gain control



Thin bed tuning and the wedge model



(Partyka, 2001)

Summary

- **Seismic data are band-limited, limiting vertical and lateral resolution**
- **The loss of high frequencies limits our ability to resolve thin beds**
- **The loss of low frequencies limits our ability to estimate the actual value of impedance, and hence lithology and porosity**
- **Constructive and destructive interference gives rise to the tuning frequency phenomenon, which allows us to estimate layer thicknesses below $\frac{1}{4}$ wavelength limits**